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TI-59 MAGNETIC CARD CALCULATOR SOLUTIONS TO COMPOSITE MATERIALS--ETC(U)

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AFML-TR-79-4040

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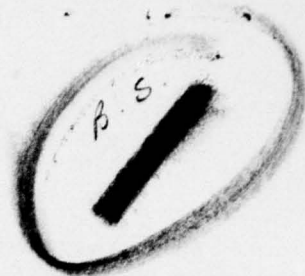


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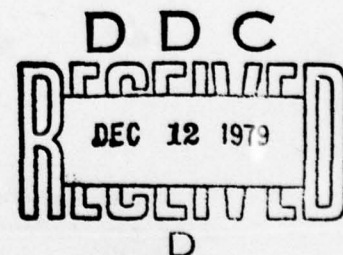
*MECHANICS AND SURFACE INTERACTIONS BRANCH
NONMETALLIC MATERIALS DIVISION*

APRIL 1979

TECHNICAL REPORT AFML-TR-79-4040
Final Report for Period October 1977 to October 1978

Approved for public release; distribution unlimited.

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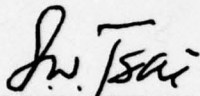
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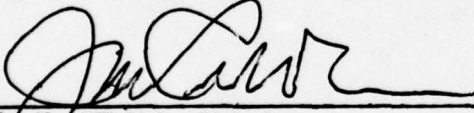
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This technical report has been reviewed and is approved for publication.



S. W. TSAI, Project Engineer & Chief
Mechanics & Surface Interactions Branch
Nonmetallic Materials Division

FOR THE COMMANDER



J. M. KELBLE, Chief
Nonmetallic Materials Division

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REPORT DOCUMENTATION PAGE		READ INSTRUCTIONS BEFORE COMPLETING FORM
1. REPORT NUMBER AFML-TR-79 - 4040	2. GOVT ACCESSION NO.	3. RECIPIENT'S CATALOG NUMBER 9
4. TITLE (and Subtitle) TI-59 MAGNETIC CARD CALCULATOR SOLUTIONS TO COMPOSITE MATERIALS FORMULAS		5. DATE OF REPORT & PERIOD COVERED Rept. for October 1977-October 1978
6. PERFORMING ORG. REPORT NUMBER		
7. AUTHOR(s) Stephen W. Tsai H. Thomas Hahn	8. CONTRACT OR GRANT NUMBER(s) N/A	
9. PERFORMING ORGANIZATION NAME AND ADDRESS Mechanics & Surface Interactions Branch Air Force Materials Division (AFML/MBM) Air Force Wright Aeronautical Laboratories Wright-Patterson AFB, Ohio 45433	10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS 24190310 12 54	
11. CONTROLLING OFFICE NAME AND ADDRESS Same as Block 9	12. REPORT DATE 11 Apr 1979	
14. MONITORING AGENCY NAME & ADDRESS (if different from Controlling Office) 62102 F	13. NUMBER OF PAGES 47	
	15. SECURITY CLASS. (of this report) UNCLASSIFIED	
	15a. DECLASSIFICATION/DOWNGRADING SCHEDULE	
16. DISTRIBUTION STATEMENT (of this Report) Approved for public release; distribution unlimited. 16 2419 17 03		
17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)		
18. SUPPLEMENTARY NOTES		
19. KEY WORDS (Continue on reverse side if necessary and identify by block number) Magnetic Card Programs Composite Materials Properties of Unidirectional & Laminated Composites In-Plane and Flexural Stiffness & Strength Nonmechanical Strains		
20. ABSTRACT (Continue on reverse side if necessary and identify by block number) This volume contains the description and instructions of magnetic cards for TI-59 programmable calculators. These tapes contain the key calculations of the stiffness and strength of unidirectional and symmetrically laminated composites. Both in-plane and flexural loadings can be applied. The initial		

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stress and strain due to curing and moisture adsorption are also included in the strength calculation. With the aid of the magnetic cards, instant calculations can be made for practical use. The use of cards is also an effective teaching tool. The formulas used in the cards have been derived in another AFML report, entitled, "Introduction to Composite Materials", AFML-TR-78-201.

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FOREWORD

This report was prepared in the Mechanics and Surface Interactions Branch (AFML/MBM), Nonmetallic Materials Division, Air Force Materials Laboratory, Wright-Patterson AFB, Ohio. The work was performed under the support Project No. 2419, "Nonmetallic Structural Materials," Task No. 241903, "Composite Materials and Mechanics Technology." The time period covered by this effort was from October 1977 to October 1978. Stephen W. Tsai (AFML/MBM) was the laboratory project engineer. H. Thomas Hahn was a member of AFML/MBM until 1 August 1978.

The page numbers which appear in the flow charts refer to the pages of this report. The equation number, however, refer to those equations in AFML-TR-78-201, "Introduction to Composite Materials".

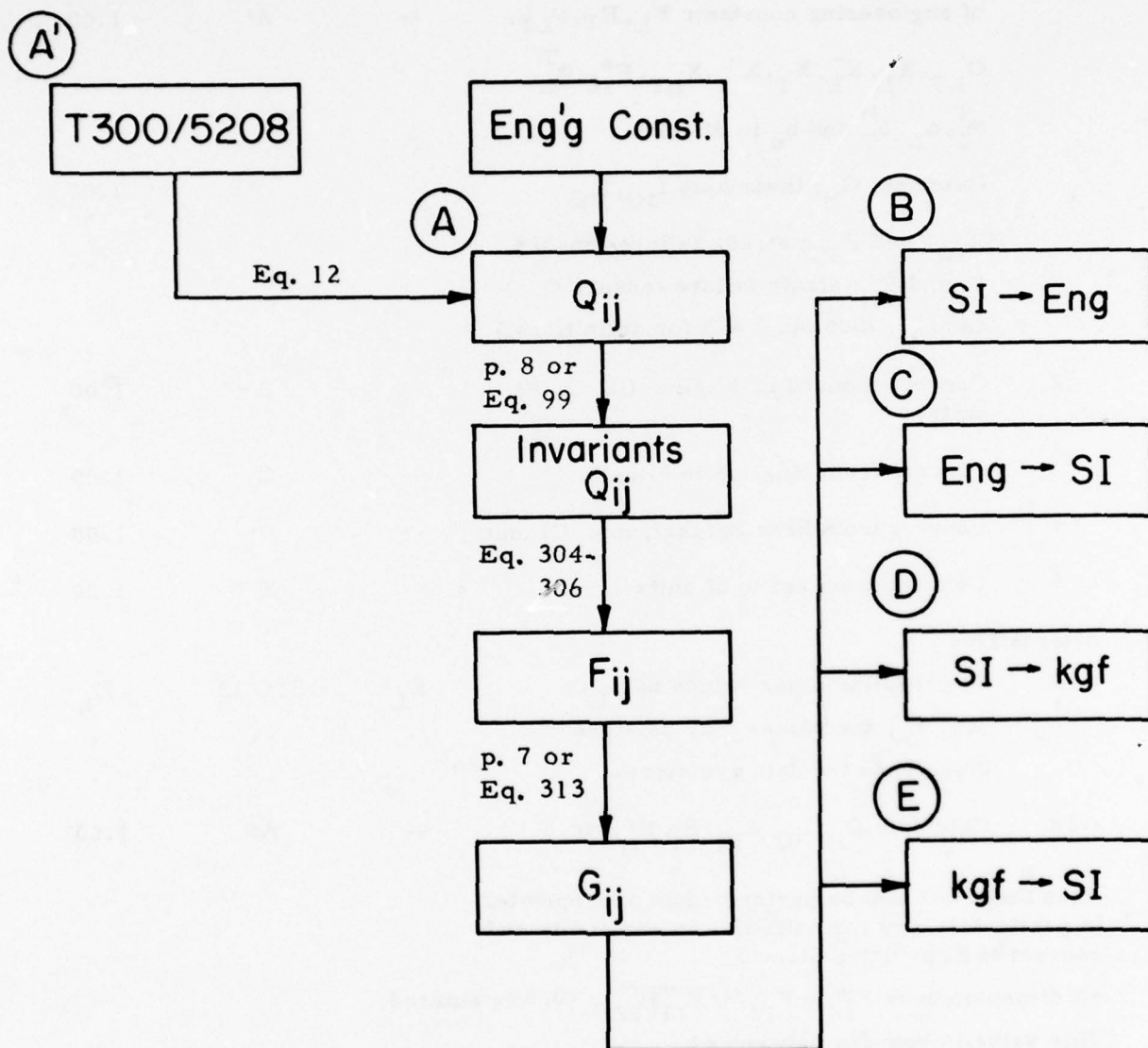
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TAPE #1
PROPERTIES OF UNIDIRECTIONAL COMPOSITES



USER INSTRUCTIONS

TAPE #1: PROPERTIES OF UNIDIRECTIONAL COMPOSITES

STEP	PROCEDURE	ENTER	PRESS	DISPLAY
1	For T300/5208 plies, initialize values of engineering constants $E_L, E_T, \nu_{LT}, G_{LT}, X_L, X_L^-, X_T, X_T^-, X_{LT}, F_{12}^*, \alpha_L^T, \alpha_T^T, \alpha_L^H, \alpha_T^H$ and h_o in SI units. Calculate Q_{ij} ; invariants I_{1Q}, I_{2Q} R_{1Q} and R_{2Q} ; stress failure tensors F_i and F_{ij} ; strain failure tensors G_i and G_{ij} . (See pp. 7 & 8 for definitions.)	--	A'	1.00
2	Convert from SI to English (lb, in, F) units.	--	B	1.00
3	Convert from English to SI units.	--	C	1.00
4	Convert from SI to kgf (kgf, mm, C) units.	--	D	1.00
5	Convert from kgf to SI units	--	E	1.00
Alternatives				
1A	To initialize other values of E_L, \dots, h_o , the values may be stored directly in the data registers.	E_L . ' .	STO 18 . .	E_L . .
2A	Calculate $Q_{ij}, I_{1Q}, R_{1Q}, F_i, F_{ij}$, etc.	--	A	1.00

Then Steps 2-5 can be performed as appropriate. In particular, one can initialize in eng. units and convert to SI by using Step 3.

A dimensionless $F_{12}^ = F_{12} / \sqrt{F_{11} F_{22}} = -0.5$ is entered.

This value is bounded between ± 1 .

Computed ply data should be recorded in blocks 3 and 4 for future use. Tape #1 need not be run, unless a change in unit (e.g. from SI to Eng) or change in properties is desired.

Tape* 1Title PROPERTIES OF UNIDIRECTIONAL COMPOSITES
(T300/5208)

KEYS	STORAGE MEMORIES			
A Initialize(after entering Eng'g Constants)	0	20	ν_{LT}	40
	1 Q_{11}	21	G_{LT}	41 h_o
A' Initialize T300/5208 (SI)	2 Q_{22}	22	α_L^T	42 I_{1Q}
	3 Q_{12}	23	α_T^T	43 I_{2Q}
B SI \rightarrow English (Pa) (psi)	4	24	α_L^H	44 R_{1Q}
	5	25	α_T^H	45 R_{2Q}
B'	6	26		46 F_{11}
	7	27	Q_{11}	47 F_1
C Eng \rightarrow SI (psi) (Pa)	8	28	Q_{22}	48 F_{22}
	9	29	Q_{12}	49 F_2
C'	10	30	Q_{66}	50 $F_{12}^* = F_{12} / \sqrt{F_{11} F_{22}}$
	11	31		51 F_{12}
D SI \rightarrow kgf (Pa) (kgf/mm ²)	12	32		52
	13 x_L	33		53
D'	14 x_L^-	34		54 G_{11}
	15 x_T	35		55 G_{22}
E kgf \rightarrow SI (kgf/mm ²) (Pa)	16 x_T^-	36		56 G_{12}
	17 x_{LT}	37		57 G_{66}
E'	18 E_L	38		58 G_1
	19 E_T	39	m	59 G_2

Tape #1 Properties of Unidirectional

T360-5208

000	76	LBL
001	16	H'
002	01	1
003	08	8
004	66	PAU
005	57	ENG
006	01	1
007	08	8
008	01	1
009	52	EE
010	09	9
011	42	STD
012	18	18
013	01	1
014	00	0
015	03	3
016	52	EE
017	08	8
018	42	STD
019	19	19
020	93	.
021	02	2
022	08	8
023	42	STD
024	20	20
025	07	7
026	01	1
027	07	7
028	52	EE
029	07	7
030	42	STD
031	21	21
032	01	1
033	05	5
034	52	EE
035	08	8
036	42	STD
037	13	13
038	42	STD
039	14	14
040	04	4
041	52	EE
042	07	7
043	42	STD
044	15	15
045	02	2
046	04	4
047	06	6
048	52	EE
049	06	6
050	42	STD
051	16	16
052	06	6
053	08	8
054	52	EE
055	06	6
056	42	STD
057	17	17
058	93	.
059	05	5
060	94	+/-
061	42	STD
062	50	50
063	01	1
064	52	EE
065	94	+/-
066	08	8
067	42	STD
068	22	22
069	01	1
070	02	2
071	05	5
072	52	EE
073	94	+/-
074	07	7
075	42	STD
076	23	23
077	00	0
078	42	STD
079	24	24

080	93	.
081	06	6
082	42	STD
083	25	25
084	01	1
085	02	2
086	05	5
087	52	EE
088	94	+/-
089	06	6
090	42	STD
091	41	41
092	76	LBL
093	11	H
094	57	ENG
095	43	RCL
096	20	20
097	33	X ²
098	65	X
099	43	RCL
100	19	19
101	55	+
102	43	RCL
103	18	18
104	75	-
105	01	1
106	95	=
107	94	+/-
108	35	1/X
109	42	STD
110	39	39
111	65	X
112	43	RCL
113	18	18
114	95	=
115	42	STD
116	27	27
117	42	STD
118	01	01
119	43	RCL
120	39	39
121	65	X
122	43	RCL
123	19	19
124	95	=
125	42	STD
126	28	28
127	42	STD
128	02	02
129	65	X
130	43	RCL
131	20	20
132	95	=
133	42	STD
134	29	29
135	42	STD
136	03	03
137	43	RCL
138	21	21
139	42	STD
140	30	30
141	65	X
142	04	4
143	75	-
144	02	2
145	65	X
146	43	RCL
147	29	29
148	85	+
149	43	RCL
150	27	27
151	85	+
152	43	RCL
153	28	28
154	95	=
155	55	+
156	08	8
157	95	=
158	42	STD
159	43	43

160	75	-
161	43	RCL
162	30	30
163	95	=
164	42	STD
165	45	45
166	43	RCL
167	27	27
168	85	+
169	43	RCL
170	28	28
171	85	+
172	02	2
173	65	X
174	43	RCL
175	29	29
176	95	=
177	55	+
178	04	4
179	95	=
180	42	STD
181	42	42
182	43	RCL
183	27	27
184	75	-
185	43	RCL
186	28	28
187	95	=
188	50	1/X
189	55	+
190	02	2
191	95	=
192	42	STD
193	44	44
194	43	RCL
195	13	13
196	65	X
197	43	RCL
198	14	14
199	95	=
200	35	1/X
201	42	STD
202	46	46
203	65	X
204	43	RCL
205	14	14
206	75	-
207	43	RCL
208	14	14
209	35	1/X
210	95	=
211	42	STD
212	47	47
213	43	RCL
214	15	15
215	65	X
216	43	RCL
217	16	16
218	95	=
219	35	1/X
220	42	STD
221	48	48
222	65	X
223	43	RCL
224	46	46
225	95	=
226	34	FX
227	65	X
228	43	RCL
229	50	50
230	95	=
231	42	STD
232	51	51
233	43	RCL
234	15	15
235	35	1/X
236	75	-
237	43	RCL
238	16	16
239	35	1/X

Tape #1 Properties of Unidirectional

Gij

240	95	=
241	42	STD
242	49	49
243	43	RCL
244	30	30
245	55	+
246	43	RCL
247	17	17
248	95	=
249	33	X ²
250	42	STD
251	57	57
252	43	RCL
253	46	46
254	65	X
255	43	RCL
256	27	27
257	33	X ²
258	85	+
259	02	2
260	65	X
261	43	RCL
262	51	51
263	65	X
264	43	RCL
265	27	27
266	65	X
267	43	RCL
268	29	29
269	85	+
270	43	RCL
271	48	48
272	65	X
273	43	RCL
274	33	29
275	33	X ²
276	95	=
277	42	STD
278	54	54
279	43	RCL
280	46	46
281	65	X
282	43	RCL
283	29	29
284	33	X ²
285	85	+
286	02	2
287	65	X
288	43	RCL
289	51	51
290	65	X
291	43	RCL
292	29	29
293	65	X
294	43	RCL
295	28	28
296	85	+
297	43	RCL
298	48	48
299	65	X
300	43	RCL
301	28	28
302	33	X ²
303	95	=
304	42	STD
305	55	55
306	43	RCL
307	46	46
308	65	X
309	43	RCL
310	27	27
311	65	X
312	43	RCL
313	29	29
314	85	+
315	43	RCL
316	51	51
317	65	X
318	43	RCL
319	27	27

320	65	X
321	43	RCL
322	28	28
323	85	+
324	43	RCL
325	51	51
326	65	X
327	43	RCL
328	29	29
329	33	X ²
330	85	+
331	43	RCL
332	48	48
333	65	X
334	43	RCL
335	28	28
336	65	X
337	43	RCL
338	29	29
339	95	=
340	42	STD
341	56	56
342	43	RCL
343	47	47
344	65	X
345	43	RCL
346	27	27
347	85	+
348	43	RCL
349	49	49
350	65	X
351	43	RCL
352	29	29
353	95	=
354	42	STD
355	58	58
356	43	RCL
357	47	47
358	65	X
359	43	RCL
360	29	29
361	85	+
362	43	RCL
363	49	49
364	65	X
365	43	RCL
366	28	28
367	95	=
368	42	STD
369	59	59
370	01	1
371	95	=
372	91	R/S
373	76	LBL
374	12	8
375	06	6
376	08	8
377	09	9
378	05	5
379	35	1/X
380	42	STD
381	40	40
382	05	5
383	55	+
384	09	9
385	95	=
386	49	PRD
387	22	22
388	49	PRD
389	23	23
390	03	3
391	09	9
392	93	.
393	04	4
394	49	PRD
395	41	41
396	71	SBR
397	34	FX
398	76	LBL
399	13	C

400	06	6
401	08	8
402	09	9
403	05	5
404	42	STD
405	40	40
406	09	9
407	55	+
408	05	5
409	95	=
410	49	PRD
411	22	22
412	49	PRD
413	23	23
414	03	3
415	09	9
416	93	.
417	04	4
418	35	1/X
419	49	PRD
420	41	41
421	71	SBR
422	34	FX
423	76	LBL
424	14	D
425	09	9
426	08	8
427	01	1
428	52	EE
429	04	4
430	35	1/X
431	42	STD
432	40	40
433	01	1
434	52	EE
435	03	3
436	49	PRD
437	41	41
438	76	LBL
439	34	FX
440	43	RCL
441	40	40
442	49	PRD
443	13	13
444	49	PRD
445	14	14
446	49	PRD
447	15	15
448	49	PRD
449	16	16
450	49	PRD
451	17	17
452	49	PRD
453	18	18
454	49	PRD
455	19	19
456	49	PRD
457	21	21
458	61	GTD
459	00	00
460	92	92
461	76	LBL
462	15	E
463	09	9
464	08	8
465	01	1
466	52	EE
467	04	4
468	42	STD
469	40	40
470	01	1
471	52	EE
472	03	3
473	35	1/X
474	49	PRD
475	41	41
476	71	SBR
477	34	FX
478	00	0
479	00	0

Tape #1 Properties of Unidirectional/Sample Problems

T300/5208

SI

ENG.

0. 00	0. 00	00
181.81114 09	26.368548 06	01
10.346159 09	1.5005306 06	02
2.8969244 09	420.14858 03	03
0. 00	0. 00	04
0. 00	0. 00	05
0. 00	0. 00	06
0. 00	0. 00	07
0. 00	0. 00	08
0. 00	0. 00	09
0. 00	0. 00	10
0. 00	0. 00	11
0. 00	0. 00	12
1.5 09	217.54895 03	13
1.5 09	217.54895 03	14
40. 06	5.8013053 03	15
246. 06	35.678028 03	16
68. 06	9.862219 03	17
181. 09	26.250906 06	18
10.3 09	1.4938361 06	19
280. -03	280. -03	20
7.17 09	1.039884 06	21
10. -09	5.5555556 -09	22
12.5 -06	6.9444444 -06	23
0. 00	0. 00	24
600. -03	600. -03	25
0. 00	0. 00	26
181.81114 09	26.368548 06	27
10.346159 09	1.5005306 06	28
2.8969244 09	420.14858 03	29
7.17 09	1.039884 06	30
0. 00	0. 00	31
0. 00	0. 00	32
0. 00	0. 00	33
0. 00	0. 00	34
0. 00	0. 00	35
0. 00	0. 00	36
0. 00	0. 00	37
0. 00	0. 00	38
1.0044814 00	1.0044814 00	39
0. 00	145.03263 -06	40
125. -06	4.92125 -03	41
49.487787 09	7.177344 06	42
26.880431 09	3.8985397 06	43
85.73249 09	12.434009 06	44
19.710431 09	2.8586557 06	45
444.44444 -21	21.129344 -12	46
0. 00	-1. -18	47
101.62602 -18	4.831405 -09	48
20.934959 09	144.34654 -06	49
-500. -03	-500. -03	50
-3.3603243 -18	-154.75326 -12	51
0. 00	0. 00	52
0. 00	0. 00	53
12.004384 03	12.004384 03	54
10.680652 03	10.680652 03	55
3.0691032 03	-3.0691032 03	56
11.117842 03	11.117842 03	57
60.646995 00	60.646995 00	58
216.59641 00	216.59641 00	59

AS/3501

SI

ENG.

0. 00	0. 00	00
138.78041 09	20.127688 06	01
9.0162185 09	1.3076459 06	02
2.7048656 09	392.29377 03	03
0. 00	0. 00	04
0. 00	0. 00	05
0. 00	0. 00	06
0. 00	0. 00	07
0. 00	0. 00	08
0. 00	0. 00	09
0. 00	0. 00	10
0. 00	0. 00	11
0. 00	0. 00	12
1.44795 09	210. 03	13
1.44795 09	210. 03	14
51.7125 06	7.5 03	15
206.85 06	30. 03	16
93.0825 06	13.5 03	17
137.96895 09	20.01 06	18
8.9635 09	1.3 06	19
300. -03	300. -03	20
7.10185 09	1.03 06	21
10. -09	5.5555556 -09	22
12.5 -06	6.9444444 -06	23
0. 00	0. 00	24
600. -03	600. -03	25
0. 00	0. 00	26
138.78041 09	20.127688 06	27
9.0162185 09	1.3076459 06	28
2.7048656 09	392.29377 03	29
7.10185 09	1.03 06	30
0. 00	0. 00	31
0. 00	0. 00	32
0. 00	0. 00	33
0. 00	0. 00	34
0. 00	0. 00	35
0. 00	0. 00	36
0. 00	0. 00	37
0. 00	0. 00	38
1.0058815 00	1.0058815 00	39
6.895 03	145.03263 -06	40
133.24846 -06	5.2499895 -03	41
38.30159 09	5.5549804 06	42
21.349287 09	3.0963433 06	43
64.882096 09	9.4100211 06	44
14.247437 09	2.0663433 06	45
476.97198 -21	22.675737 -12	46
-100. -24	0. 00	47
93.486509 -18	4.4444444 -09	48
14.503263 -09	100. -06	49
-500. -03	-500. -03	50
-3.3388039 -18	-158.73016 -12	51
0. 00	0. 00	52
0. 00	0. 00	53
7.3638004 03	7.3638004 03	54
7.4403621 03	7.4403621 03	55
-1.7432239 03	-1.7432239 03	56
5.8211248 03	5.8211248 03	57
39.229377 00	39.229377 00	58
130.76459 00	130.76459 00	59

TAPE #1

TENSOR POLYNOMIAL FAILURE CRITERION IN STRAIN SPACE

Find: $G_{ij} e_i e_j + G_i e_i = 1$

From: $F_{ij} \sigma_i \sigma_j + F_i \sigma_i = 1$

and $\sigma_i = Q_{ij} e_j$

we have $G_{ij} = Q_{ik} Q_{jl} F_{kl}$

$$G_i = Q_{ik} F_k$$

For orthotropic materials: $Q_{16} = Q_{26} = 0$

$$G_{11} = F_{11} Q_{11}^2 + 2F_{12} Q_{11} Q_{21} + F_{22} Q_{12}^2$$

$$G_{22} = F_{11} Q_{12}^2 + 2F_{12} Q_{12} Q_{22} + F_{22} Q_{22}^2$$

$$G_{66} = F_{66} Q_{66}^2 = \left(\frac{Q_{66}}{X_{LT}} \right)^2$$

$$G_{12} = F_{11} Q_{11} Q_{12} + F_{12} (Q_{11} Q_{22} + Q_{12}^2) + F_{22} Q_{21} Q_{22}$$

$$G_{16} = G_{26} = 0$$

$$G_1 = F_1 Q_{11} + F_2 Q_{21}$$

$$G_2 = F_1 Q_{12} + F_2 Q_{22}$$

$$G_6 = 0$$

TAPE #1

DEFINITIONS OF INVARIANTS OF ELASTIC MODULUS

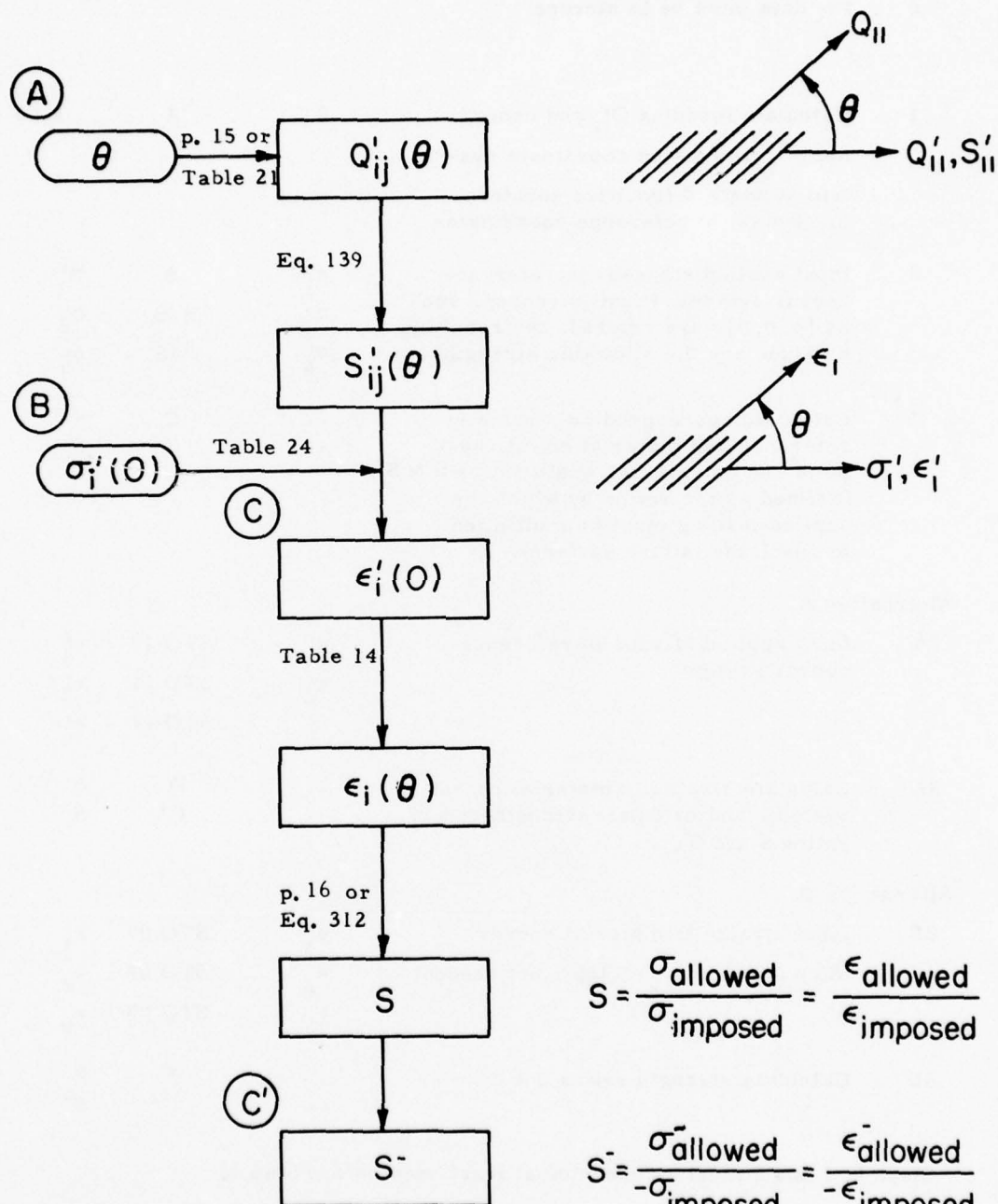
$$I_{1Q} = \frac{1}{2}(Q_{11} + Q_{22} - 2Q_{12}) = (U_1 + U_4) / 2$$

$$I_{2Q} = \frac{1}{4}(Q_{11} + Q_{22} - 2Q_{12} + 4Q_{66}) = U_5 = (U_1 - U_4) / 2$$

$$R_{1Q} = U_2$$

$$R_{2Q} = U_3$$

TAPE #2 OFF-AXIS PROPERTIES OF UNIDIRECTIONAL COMPOSITES



USER INSTRUCTIONS

TAPE #2: OFF-AXIS PROPERTIES OF UNIDIRECTIONAL COMPOSITES

STEP	PROCEDURE	ENTER	PRESS	DISPLAY
0	Ply data must be in storage			
1	Calculate modulus Q'_{ij} and compliance S'_{ij} in rotated coordinate system at angle θ (positive counter-clockwise) to reference coordinates	θ	A	1.00
2	Input applied stresses in reference coord. system. If unit stresses, such as [1, 0, 0], are entered, the resulting S values are the allowable strengths.	σ'_1 σ'_2 σ'_6	B R/S R/S	σ'_1 σ'_2 σ'_6
3*	Calculate corresponding strains in reference and material coord. systems and calculate strength ratios S & S^- . (defined as the ratios by which the applied loading must be multiplied to reach the failure surface).	-- --	C C'	S S^-

Alternative A

2A	Input applied strains in reference coord. system	ϵ'_1 ϵ'_2 ϵ'_6	STO 10 STO 11 STO 12	ϵ'_1 ϵ'_2 ϵ'_6
3A	Calculate strains in material coord. system, and calculate strength-strain ratios S and S^- .	-- --	D C'	S S^-

Alternative B

2B	Input strains in material coords. (Step 0 needed, but Step 1 not needed)	ϵ_1 ϵ_2 ϵ_6	STO 07 STO 08 STO 09	ϵ_1 ϵ_2 ϵ_6
3B	Calculate strength ratios S & S^- .	-- --	E C'	S S^-

- * Steps 0, 1 and 2 must be executed at least once before Step 3.
If only the angle in Step 1 is changed while the stress remains the same Step 2 can be skipped. If the stress is changed while the angle remains constant, Step 1 can be omitted.

Tape* 2Title OFF-AXIS PROPERTIES OF UNIDIRECTIONAL COMPOSITES

KEYS	STORAGE MEMORIES			
A θ	0	θ	20	40 4θ
	1	σ'_1	21	41 h_o
A'	2	σ'_2	22	42 I_{1Q}
	3	σ'_6	23	43 I_{2Q}
B σ'_i	4		24	44 R_{1Q}
	5		25	45 R_{2Q}
B'	6		26 $ Q $	46
	7	e_1	27 Q'_{11}	47
C S	8	e_2	28 Q'_{22}	48
	9	e_6	29 Q'_{12}	49
C' S^-	10	e'_1	30 Q'_{66}	50
	11	e'_2	31 Q'_{16}	51
D S from e'_i	12	e'_6	32 Q'_{26}	52 ... S
	13		33 S'_{11}	53 ... S^-
D'	14		34 S'_{22}	54 G_{11}
	15		35 S'_{12}	55 G_{22}
E S from e_i	16		36 S'_{66}	56 G_{12}
	17		37 S'_{16}	57 G_{66}
E'	18		38 S'_{26}	58 G_1
	19		39 2θ	59 G_2

Tape #2 Off-Axis Properties

θ
 000 76 LBL
 001 11 A
 002 57 ENG
 003 42 STD
 004 00 00
 005 65 x
 006 02 2
 007 95 =
 008 42 STD
 009 39 39
 010 65 x
 011 02 2
 012 95 =
 013 42 STD
 014 40 40
 015 01 1
 016 06 6
 017 66 PAU

 018 43 RCL
 019 42 42
 020 85 +
 021 43 RCL
 022 43 43
 023 85 +
 024 43 RCL
 025 39 39
 026 39 CDS
 027 65 x
 028 43 RCL
 029 44 44
 030 85 +
 031 43 RCL
 032 40 40
 033 39 CDS
 034 65 x
 035 43 RCL
 036 45 45
 037 95 =
 038 42 STD
 039 27 27
 040 75 -
 041 43 RCL
 042 39 39
 043 39 CDS
 044 65 x
 045 02 2
 046 65 x
 047 43 RCL
 048 44 44
 049 95 =
 050 42 STD
 051 28 28
 052 43 RCL
 053 42 42
 054 75 -
 055 43 RCL
 056 43 43
 057 75 -
 058 43 RCL
 059 40 40
 060 39 CDS
 061 65 x
 062 43 RCL
 063 45 45
 064 95 =
 065 42 STD
 066 29 29
 067 85 +
 068 02 2
 069 65 x
 070 43 RCL
 071 43 43
 072 75 -
 073 43 RCL
 074 42 42
 075 95 =
 076 42 STD
 077 30 30
 078 43 RCL
 079 39 39

Q'_{ij}

IQI

S'_{ij}

080 38 SIN
 081 55 +
 082 02 2
 083 65 x
 084 43 RCL
 085 44 44
 086 95 =
 087 85 +
 088 43 RCL
 089 40 40
 090 38 SIN
 091 65 x
 092 43 RCL
 093 45 45
 094 95 =
 095 42 STD
 096 31 31
 097 75 -
 098 43 RCL
 099 39 39
 100 38 SIN
 101 65 x
 102 43 RCL
 103 44 44
 104 95 =
 105 94 +/-
 106 42 STD
 107 32 32

 108 43 RCL
 109 27 27
 110 65 x
 111 43 RCL
 112 28 28
 113 65 x
 114 43 RCL
 115 30 30
 116 85 +
 117 43 RCL
 118 29 29
 119 65 x
 120 43 RCL
 121 31 31
 122 65 x
 123 43 RCL
 124 32 32
 125 65 x
 126 02 2
 127 75 -
 128 43 RCL
 129 28 28
 130 65 x
 131 43 RCL
 132 31 31
 133 33 X²
 134 75 -
 135 43 RCL
 136 27 27
 137 65 x
 138 43 RCL
 139 32 32
 140 33 X²
 141 75 -
 142 43 RCL
 143 30 30
 144 65 x
 145 43 RCL
 146 29 29
 147 33 X²
 148 95 =
 149 42 STD
 150 26 26

 151 43 RCL
 152 28 28
 153 65 x
 154 43 RCL
 155 30 30
 156 75 -
 157 43 RCL
 158 32 32
 159 33 X²

S'_{ij}

160 95 =
 161 42 STD
 162 33 33
 163 43 RCL
 164 27 27
 165 65 x
 166 43 RCL
 167 28 28
 168 75 -
 169 43 RCL
 170 29 29
 171 33 X²
 172 95 =
 173 42 STD
 174 36 36
 175 43 RCL
 176 27 27
 177 65 x
 178 43 RCL
 179 30 30
 180 75 -
 181 43 RCL
 182 31 31
 183 33 X²
 184 95 =
 185 42 STD
 186 34 34
 187 43 RCL
 188 29 29
 189 65 x
 190 43 RCL
 191 32 32
 192 75 -
 193 43 RCL
 194 28 28
 195 65 x
 196 43 RCL
 197 31 31
 198 95 =
 199 42 STD
 200 37 37
 201 43 RCL
 202 31 31
 203 65 x
 204 43 RCL
 205 32 32
 206 75 -
 207 43 RCL
 208 29 29
 209 65 x
 210 43 RCL
 211 30 30
 212 95 =
 213 42 STD
 214 35 35
 215 43 RCL
 216 29 29
 217 65 x
 218 43 RCL
 219 31 31
 220 75 -
 221 43 RCL
 222 27 27
 223 65 x
 224 43 RCL
 225 32 32
 226 95 =
 227 42 STD
 228 38 38

 229 43 RCL
 230 26 26
 231 35 1/X
 232 49 FRD
 233 33 33
 234 49 FRD
 235 34 34
 236 49 FRD
 237 35 35
 238 49 FRD
 239 36 36

Tape #2 Off-Axis Properties

240	49	PRD
241	37	37
242	49	PRD
243	38	38
244	01	1
245	95	=
246	91	R/S
247	76	LBL
248	12	B
249	42	STD
250	01	01
251	91	R/S
252	42	STD
253	02	02
254	91	R/S
255	12	STD
256	03	03
257	91	R/S
258	76	LBL
259	13	C
260	01	1
261	04	4
262	66	PHU
263	43	RCL
264	03	03
265	65	x
266	43	RCL
267	37	37
268	85	+
269	43	RCL
270	02	02
271	65	x
272	43	RCL
273	35	35
274	85	+
275	43	RCL
276	01	01
277	65	x
278	43	RCL
279	33	33
280	95	=
281	42	STD
282	10	10
283	43	RCL
284	01	01
285	65	x
286	43	RCL
287	35	35
288	85	+
289	43	RCL
290	02	02
291	65	x
292	43	RCL
293	34	34
294	85	+
295	43	RCL
296	03	03
297	65	x
298	43	RCL
299	38	38
300	95	=
301	42	STD
302	11	11
303	43	RCL
304	01	01
305	65	x
306	43	RCL
307	37	37
308	85	+
309	43	RCL
310	02	02
311	65	x
312	43	RCL
313	38	38
314	85	+
315	43	RCL
316	03	03
317	65	x
318	43	RCL
319	36	36

320	95	=
321	42	STD
322	12	12
323	76	LBL
324	14	D
325	43	RCL
326	00	00
327	39	COS
328	33	X ²
329	65	x
330	43	RCL
331	10	10
332	85	+
333	43	RCL
334	00	00
335	38	SIN
336	33	X ²
337	65	x
338	43	RCL
339	11	11
340	85	+
341	43	RCL
342	00	00
343	39	COS
344	65	x
345	43	RCL
346	00	00
347	38	SIN
348	65	x
349	43	RCL
350	12	12
351	95	=
352	42	STD
353	07	07
354	75	-
355	43	RCL
356	10	10
357	75	-
358	43	RCL
359	11	11
360	95	=
361	94	+/-
362	42	STD
363	08	08
364	43	RCL
365	11	11
366	75	-
367	43	RCL
368	10	10
369	95	=
370	65	x
371	43	RCL
372	39	39
373	38	SIN
374	85	+
375	43	RCL
376	39	39
377	39	COS
378	65	x
379	43	RCL
380	12	12
381	95	=
382	42	STD
383	09	09
384	76	LBL
385	15	E
386	43	RCL
387	54	54
388	65	x
389	43	RCL
390	07	07
391	33	X ²
392	85	+
393	02	2
394	65	x
395	43	RCL
396	56	56
397	65	x
398	43	RCL
399	07	07

400	65	x
401	43	RCL
402	08	08
403	85	+
404	43	RCL
405	55	55
406	65	x
407	43	RCL
408	08	08
409	33	X ²
410	85	+
411	43	RCL
412	57	57
413	65	x
414	43	RCL
415	09	09
416	33	X ²
417	95	=
418	42	STD
419	52	52
420	43	RCL
421	58	58
422	65	x
423	43	RCL
424	07	07
425	85	+
426	43	RCL
427	59	59
428	65	x
429	43	RCL
430	08	08
431	95	=
432	42	STD
433	53	53
434	43	RCL
435	52	52
436	35	1/X
437	42	STD
438	52	52
439	65	x
440	43	RCL
441	53	53
442	55	+
443	02	2
444	95	=
445	42	STD
446	53	53
447	33	X ²
448	85	+
449	43	RCL
450	52	52
451	95	=
452	34	FX
453	42	STD
454	52	52
455	85	+
456	43	RCL
457	53	53
458	95	=
459	94	+/-
460	42	STD
461	53	53
462	85	+
463	02	2
464	65	x
465	43	RCL
466	52	52
467	95	=
468	42	STD
469	52	52
470	91	R/S
471	76	LBL
472	18	C
473	43	RCL
474	53	53
475	91	R/S
476	00	0
477	00	0
478	00	0
479	00	0

Tape #2 Off-Axis Properties/Sample Problems

θ	0.00	15.00	00	30.00	45.00	00
σ_i	1.00	1.00	01	1.00	1.00	01
	0.00	0.00	02	0.00	0.00	02
	0.00	0.00	03	0.00	0.00	03
	0.00	0.00	04	0.00	0.00	04
	0.00	0.00	05	0.00	0.00	05
	0.00	0.00	06	0.00	0.00	06
	5.5248619-12	5.0511395-12	07	3.7569061-12	1.9889503-12	07
	-1.5469613-12	5.0602866-12	08	23.111624-12	47.770209-12	08
	0.00	-34.867503-12	09	-60.392288-12	-69.735007-12	09
	5.5248619-12	13.768628-12	10	34.746213-12	59.747083-12	10
	-1.5469613-12	-3.657202-12	11	-7.8776833-12	-9.987924-12	11
	0.00	-30.200717-12	12	-46.957821-12	-45.781258-12	12
	1.5 09	1.5 09	13	1.5 09	1.5 09	13
	1.5 09	1.5 09	14	1.5 09	1.5 09	14
	40.06	40.06	15	40.06	40.06	15
	246.06	246.06	16	246.06	246.06	16
	68.06	68.06	17	68.06	68.06	17
	181.09	181.09	18	181.09	181.09	18
	10.3 09	10.3 09	19	10.3 09	10.3 09	19
	280.-03	280.-03	20	280.-03	280.-03	20
	7.17 09	7.17 09	21	7.17 09	7.17 09	21
	10.-09	10.-09	22	10.-09	10.-09	22
	12.5-06	12.5-06	23	12.5-06	12.5-06	23
	0.00	0.00	24	0.00	0.00	24
	600.-03	600.-03	25	600.-03	600.-03	25
	13.426934 30	13.426934 30	26	13.426934 30	13.426934 30	26
	181.81114 09	160.46395 09	27	109.37925 09	56.657787 09	27
	10.346159 09	11.976919 09	28	23.646757 09	56.657787 09	28
	2.8969244 09	12.75214 09	29	32.462571 09	42.317787 09	29
	7.17 09	17.025216 09	30	36.735647 09	46.590862 09	30
	0.00	38.502857 09	31	54.192991 09	42.866245 09	31
	0.00	4.3633885 09	32	20.053523 09	42.866245 09	32
	5.5248619-12	13.768628-12	33	34.746213-12	59.747083-12	33
	97.087379-12	93.064094-12	34	80.527471-12	59.747083-12	34
	-1.5469613-12	-3.657202-12	35	-7.8776833-12	-9.987924-12	35
	139.47001-12	131.02905-12	36	114.14713-12	105.70616-12	36
	0.00	-30.200717-12	37	-46.957821-12	-45.781258-12	37
	0.00	-15.580541-12	38	-32.337645-12	-45.781258-12	38
	0.00	30.00	39	60.00	90.00	39
	0.00	60.00	40	120.00	180.00	40
	125.-06	125.-06	41	125.-06	125.-06	41
	49.487787 09	49.487787 09	42	49.487787 09	49.487787 09	42
	26.880431 09	26.880431 09	43	26.880431 09	26.880431 09	43
	85.73249 09	85.73249 09	44	85.73249 09	85.73249 09	44
	19.710431 09	19.710431 09	45	19.710431 09	19.710431 09	45
	444.44444-21	444.44444-21	46	444.44444-21	444.44444-21	46
	0.00	0.00	47	0.00	0.00	47
	101.62602-18	101.62602-18	48	101.62602-18	101.62602-18	48
	20.934959-09	20.934959-09	49	20.934959-09	20.934959-09	49
	-500.-03	-500.-03	50	-500.-03	-500.-03	50
	-3.3603243-18	-3.3603243-18	51	-3.3603243-18	-3.3603243-18	51
	1.5 09	222.22216 06	52	101.22462 06	64.536588 06	52
	1.5 09	322.82798 06	53	215.27228 06	198.9018 06	53
	12.004384 03	12.004384 03	54	12.004384 03	12.004384 03	54
	10.680652 03	10.680652 03	55	10.680652 03	10.680652 03	55
	-3.0691032 03	-3.0691032 03	56	-3.0691032 03	-3.0691032 03	56
	11.117842 03	11.117842 03	57	11.117842 03	11.117842 03	57
	60.646995 00	60.646995 00	58	60.646995 00	60.646995 00	58
	216.59641 00	216.59641 00	59	216.59641 00	216.59641 00	59

TAPE #2

TRANSFORMATION OF MODULUS COMPONENTS

	I_{1Q}	I_{2Q}	R_{1Q}	R_{2Q}
Q'_{11}	1	1	$\cos 2\theta$	$\cos 4\theta$
Q'_{22}	1	1	$-\cos 2\theta$	$\cos 4\theta$
Q'_{12}	1	-1		$-\cos 4\theta$
Q'_{66}		1		$-\cos 4\theta$
Q'_{16}			$\frac{1}{2}\sin 2\theta$	$\sin 4\theta$
Q'_{26}			$\frac{1}{2}\sin 2\theta$	$-\sin 4\theta$

$$Q'_{22} = Q'_{11} - 2R_{1Q}\cos 2\theta$$

$$Q'_{26} = Q'_{16} - 2R_{2Q}\sin 4\theta$$

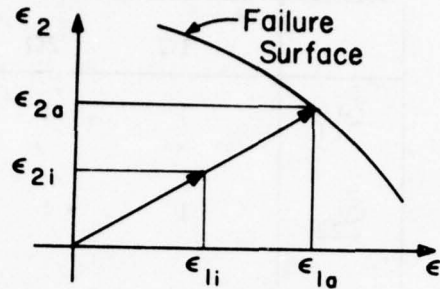
TAPE #2

STRENGTH RATIOS FOR UNIDIRECTIONAL COMPOSITES

Define $S = \frac{\epsilon_{\text{allowed}}}{\epsilon_{\text{imposed}}} = \frac{\epsilon_a}{\epsilon_i}$

Proportional loading is assumed; i.e.

$$\frac{\epsilon_{1a}}{\epsilon_{1i}} = \frac{\epsilon_{2a}}{\epsilon_{2i}} = \frac{\epsilon_{6a}}{\epsilon_{6i}} = S$$



Since linearly elastic behavior up to failure is also assumed,

$$S = \frac{\epsilon_a}{\epsilon_i} = \frac{\sigma_{\text{allowed}}}{\sigma_{\text{imposed}}}$$

Failure occurs when $\epsilon_{\text{imposed}} = \epsilon_{\text{allowed}}$, the failure criterion is satisfied:

$$G_{ij} \epsilon_i \epsilon_j + G_i \epsilon_i = 1$$

Then strength ratio $S = 1$.

If $\epsilon_{\text{imposed}}$ is less than $\epsilon_{\text{allowed}}$, $S > 1$. The failure criterion is also satisfied:

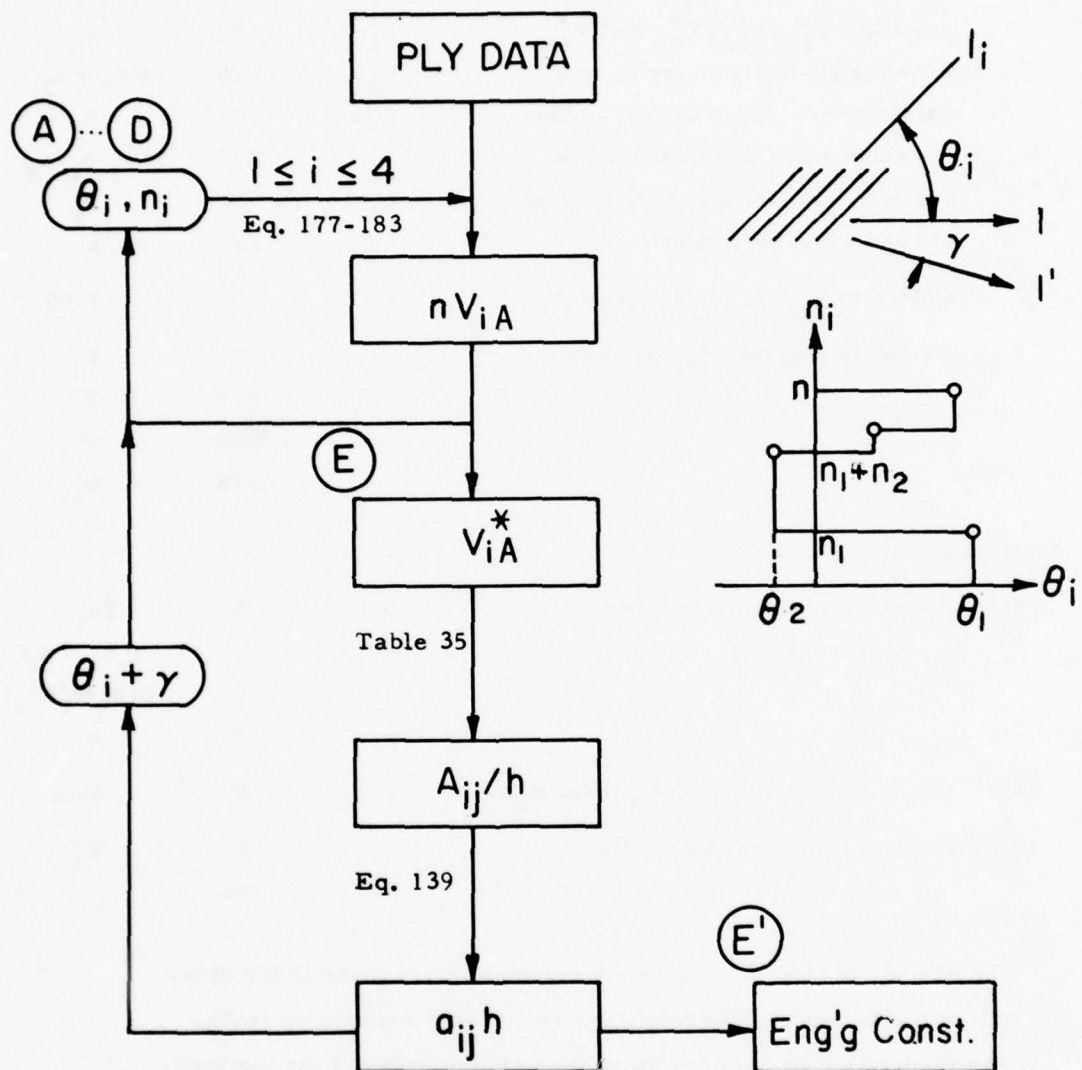
$$G_{ij} \epsilon_i \epsilon_j S^2 + G_i \epsilon_i S = 1$$

where strains in this equation are $\epsilon_{\text{imposed}}$.

For a given state of imposed strains, we can solve for the quadratic equation for S ; the other real root is the strength ratio S^- which corresponds to that when all the imposed strains change signs. If original ϵ_i were all positive, the S^- is the strength ratio for opposite strains, or $-\epsilon_i$.

TAPE #3

IN-PLANE STIFFNESS OF SYMMETRIC LAMINATES



USER INSTRUCTIONS

TAPE #3: IN-PLANE STIFFNESS OF SYMMETRIC LAMINATES

STEP	PROCEDURE	ENTER	PRESS	DISPLAY
0	Enter ply data.	--		
1	Enter ply angle θ_i , and number of plies at that angle, n_i^* , $i=1, 4$, and calculate V_{1A}^* , V_{2A}^* , V_{3A}^* and V_{4A}^* for each ply and sum them, and calculate n . Since $1 \leq i \leq 4$, values for nonexistent plies need not be entered, i.e. for a $[0/90]$ laminate, $i=3$ and 4 can be skipped.	θ_1	A	θ_1
		n_1	R/S	$2n_1$
		θ_2	B	θ_2
		n_2	R/S	$2(n_1 + n_2)$
		θ_3	C	θ_3
		n_3	R/S	$2(n_1 + n_2 + n_3)$
		θ_4	D	θ_4
		n_4	R/S	n
2	Calculate V_{iA} , h , A_{ij}/h , and $a_{ij}h$.	--	E	1.00
3	Calculate engineering constants	--	E'	E_1^0
		--	R/S	E_2^0
		--	R/S	ν_{12}^0
		--	R/S	G_{12}^0

Alternative A

1A	Rotate entire laminate by γ ; ** n_i remain the same	γ	A'	$2n_1$
		--	B'	$2(n_1 + n_2)$
		--	C'	$2(n_1 + n_2 + n_3)$
		--	D'	n
2A	Calculate transformed A_{ij}/h and $a_{ij}h$,	--	E	1.00
3A	Calculate engineering constants	--	E'	E_1^0
		--	etc.	

* The number of plies n_i of each ply orientation are those in the upper half of the laminate. The total number for each orientation is $2n_i$. The thickness h in Register 26 is the total thickness of the laminate; the number in Register 46 is one half of the total ply number. For symmetric laminates, only the fraction of each orientation rather than the absolute number of plies is important.

** This is equivalent to rotating the reference coordinates in the clockwise or negative direction.

Tape* 3Title IN-PLANE STIFFNESS OF SYMMETRIC LAMINATES

KEYS	STORAGE MEMORIES		
A θ_1, n_1	0 γ	20 n_4	40 n_i
	1	21	41 h_o
A' $\theta_1 + \gamma, n_1$	2	22	42 I_{1Q}
	3	23	43 I_{2Q}
B θ_2, n_2	4	24	44 R_{1Q}
	5	25	45 R_{2Q}
B' $\theta_2 + \gamma, n_2$	6	26 h	46 $n/2$
	7	27 $Q_{11}, A_{11}/h$	47 V_{1A}^*
C θ_3, n_3	8	28 $Q_{22}, A_{22}/h$	48 V_{2A}^*
	9	29 $Q_{12}, A_{12}/h$	49 V_{3A}^*
C' $\theta_3 + \gamma, n_3$	10	30 $Q_{66}, A_{66}/h$	50 V_{4A}^*
	11	31 A_{16}/h	51
D θ_4, n_4	12	32 A_{26}/h	52
	13 θ_1	33 a_{11}^h	53
D' $\theta_4 + \gamma, n_4$	14 n_1	34 a_{22}^h	54
	15 θ_2	35 a_{12}^h	55
E $A_{ij}/h, a_{ij}^h$	16 n_2	36 a_{66}^h	56
	17 θ_3	37 a_{16}^h	57
E' Engineering Constants	18 n_3	38 a_{26}^h	58
	19 θ_4	39 $\theta_i, A $	59

Tape #3 In-Plane Stiffness

θ_1, n_1	000	76	LBL	080	39	CDS	160	43	RCL
	001	11	A	081	65	x	161	48	48
	002	57	ENG	082	43	RCL	162	65	x
	003	42	STD	083	40	40	163	43	RCL
	004	13	13	084	95	=	164	45	45
	005	00	0	085	44	SUM	165	95	=
	006	42	STD	086	47	47	166	42	STD
	007	46	46	087	43	RCL	167	27	27
	008	42	STD	088	39	39	168	75	-
	009	47	47	089	38	SIN	169	02	2
	010	42	STD	090	65	x	170	65	x
	011	48	48	091	43	RCL	171	43	RCL
	012	42	STD	092	40	40	172	47	47
	013	49	49	093	95	=	173	65	x
	014	42	STD	094	44	SUM	174	43	RCL
	015	50	50	095	49	49	175	44	44
	016	43	RCL	096	02	2	176	95	=
	017	13	13	097	49	PRD	177	42	STD
	018	91	R/S	098	39	39	178	28	28
	019	42	STD	099	43	RCL	179	43	RCL
	020	14	14	100	39	39	180	42	42
	021	42	STD	101	39	CDS	181	75	-
	022	40	40	102	65	x	182	43	RCL
	023	44	SUM	103	43	RCL	183	43	43
	024	46	46	104	40	40	184	75	-
	025	43	RCL	105	95	=	185	43	RCL
	026	13	13	106	44	SUM	186	48	48
	027	71	SBR	107	48	48	187	65	x
	028	33	X ²	108	43	RCL	188	43	RCL
θ_2, n_2	029	76	LBL	109	39	39	189	45	45
	030	12	B	110	38	SIN	190	95	=
	031	42	STD	111	65	x	191	42	STD
	032	15	15	112	43	RCL	192	29	29
	033	91	R/S	113	40	40	193	75	-
	034	42	STD	114	95	=	194	43	RCL
	035	16	16	115	44	SUM	195	42	42
	036	42	STD	116	50	50	196	85	+
	037	40	40	117	43	RCL	197	02	2
	038	44	SUM	118	46	46	198	65	x
	039	46	46	119	65	x	199	43	RCL
	040	43	RCL	120	02	2	200	43	43
	041	15	15	121	95	=	201	95	=
	042	71	SBR	122	91	R/S	202	42	STD
	043	33	X ²	123	76	LBL	203	30	30
θ_3, n_3	044	76	LBL	124	15	E	204	43	RCL
	045	13	C	125	01	1	205	49	49
	046	42	STD	126	03	3	206	65	x
	047	17	17	127	66	PAU	207	43	RCL
	048	91	R/S	128	43	RCL	208	44	44
	049	42	STD	129	46	46	209	55	+
	050	18	18	130	35	1/X	210	02	2
	051	42	STD	131	49	PRD	211	85	+
	052	40	40	132	47	47	212	43	RCL
	053	44	SUM	133	49	PRD	213	50	50
	054	46	46	134	48	48	214	65	x
	055	43	RCL	135	49	PRD	215	43	RCL
	056	17	17	136	49	49	216	45	45
	057	71	SBR	137	49	PRD	217	95	=
	058	33	X ²	138	50	50	218	94	+/-
θ_4, n_4	059	76	LBL	139	35	1/X	219	42	STD
	060	14	D	140	65	x	220	31	31
	061	42	STD	141	43	RCL	221	85	+
	062	19	19	142	41	41	222	02	2
	063	91	R/S	143	65	x	223	65	x
	064	42	STD	144	02	2	224	43	RCL
	065	20	20	145	95	=	225	50	50
	066	42	STD	146	42	STD	226	65	x
	067	40	40	147	26	26	227	43	RCL
	068	44	SUM	148	43	RCL	228	45	45
	069	46	46	149	42	42	229	95	=
	070	43	RCL	150	85	+	230	42	STD
	071	19	19	151	43	RCL	231	32	32
V_{IA}	072	76	LBL	152	43	43	232	43	RCL
	073	33	X ²	153	85	+	233	27	27
	074	65	x	154	43	RCL	234	65	x
	075	02	2	155	47	47	235	43	RCL
	076	95	=	156	65	x	236	28	28
	077	94	+/-	157	43	RCL	237	65	x
	078	42	STD	158	44	44	238	43	RCL
	079	39	39	159	85	+	239	30	30
				V_{IA}^*					
				A_{ij}/h		$ A $			

Tape #3 In-Plane Stiffness

240	85	+
241	43	RCL
242	29	29
243	65	x
244	43	RCL
245	31	31
246	65	x
247	43	RCL
248	32	32
249	65	x
250	02	2
251	75	-
252	43	RCL
253	28	28
254	65	x
255	43	RCL
256	31	31
257	33	X ²
258	75	-
259	43	RCL
260	27	27
261	65	x
262	43	RCL
263	32	32
264	33	X ²
265	75	-
266	43	RCL
267	30	30
268	65	x
269	43	RCL
270	29	29
271	33	X ²
272	95	=
273	42	STD
274	39	39
275	43	RCL
276	28	28
277	65	x
278	43	RCL
279	30	30
280	75	-
281	43	RCL
282	32	32
283	33	X ²
284	95	=
285	42	STD
286	33	33
287	43	RCL
288	27	27
289	65	x
290	43	RCL
291	28	28
292	75	-
293	43	RCL
294	29	29
295	33	X ²
296	95	=
297	42	STD
298	36	36
299	43	RCL
300	27	27
301	65	x
302	43	RCL
303	30	30
304	75	-
305	43	RCL
306	31	31
307	33	X ²
308	95	=
309	42	STD
310	34	34
311	43	RCL
312	29	29
313	65	x
314	43	RCL
315	32	32
316	75	-
317	43	RCL
318	28	28
319	65	x

a_{ij}*

320	43	RCL
321	31	31
322	95	=
323	42	STD
324	37	37
325	43	RCL
326	31	31
327	65	x
328	43	RCL
329	32	32
330	75	-
331	43	RCL
332	29	29
333	65	x
334	43	RCL
335	30	30
336	95	=
337	42	STD
338	35	35
339	43	RCL
340	29	29
341	65	x
342	43	RCL
343	31	31
344	75	-
345	43	RCL
346	27	27
347	65	x
348	43	RCL
349	32	32
350	95	=
351	42	STD
352	38	38
353	43	RCL
354	39	39
355	35	1/X
356	49	PRD
357	33	33
358	49	PRD
359	34	34
360	49	PRD
361	35	35
362	49	PRD
363	36	36
364	49	PRD
365	37	37
366	49	PRD
367	38	38
368	01	1
369	95	=
370	91	R/S
371	76	LBL
372	10	E'
373	43	RCL
374	33	33
375	35	1/X
376	91	R/S
377	43	RCL
378	34	34
379	35	1/X
380	91	R/S
381	43	RCL
382	35	35
383	55	+
384	43	RCL
385	33	33
386	95	=
387	94	+/-
388	91	R/S
389	43	RCL
390	36	36
391	35	1/X
392	91	R/S
393	76	LBL
394	16	R'
395	42	STD
396	00	00
397	44	SUM
398	13	13
399	44	SUM

a_{ij}h

Eng'g
Const.

e_i+r

400	15	15
401	44	SUM
402	17	17
403	44	SUM
404	19	19
405	00	0
406	42	STD
407	46	46
408	42	STD
409	47	47
410	42	STD
411	48	48
412	42	STD
413	49	49
414	42	STD
415	50	50
416	43	RCL
417	14	14
418	42	STD
419	40	40
420	44	SUM
421	46	46
422	43	RCL
423	13	13
424	71	SBR
425	33	X ²
426	76	LBL
427	17	B'
428	43	RCL
429	16	16
430	42	STD
431	40	40
432	44	SUM
433	46	46
434	43	RCL
435	15	15
436	71	SBR
437	33	X ²
438	76	LBL
439	18	C'
440	43	RCL
441	18	18
442	42	STD
443	40	40
444	44	SUM
445	46	46
446	43	RCL
447	17	17
448	71	SBR
449	33	X ²
450	76	LBL
451	19	D'
452	43	RCL
453	20	20
454	42	STD
455	40	40
456	44	SUM
457	46	46
458	43	RCL
459	19	19
460	71	SBR
461	33	X ²
462	00	0
463	00	0
464	00	0
465	00	0
466	00	0
467	00	0
468	00	0
469	00	0
470	00	0
471	00	0
472	00	0
473	00	0
474	00	0
475	00	0
476	00	0
477	00	0
478	00	0
479	00	0

e₂+r

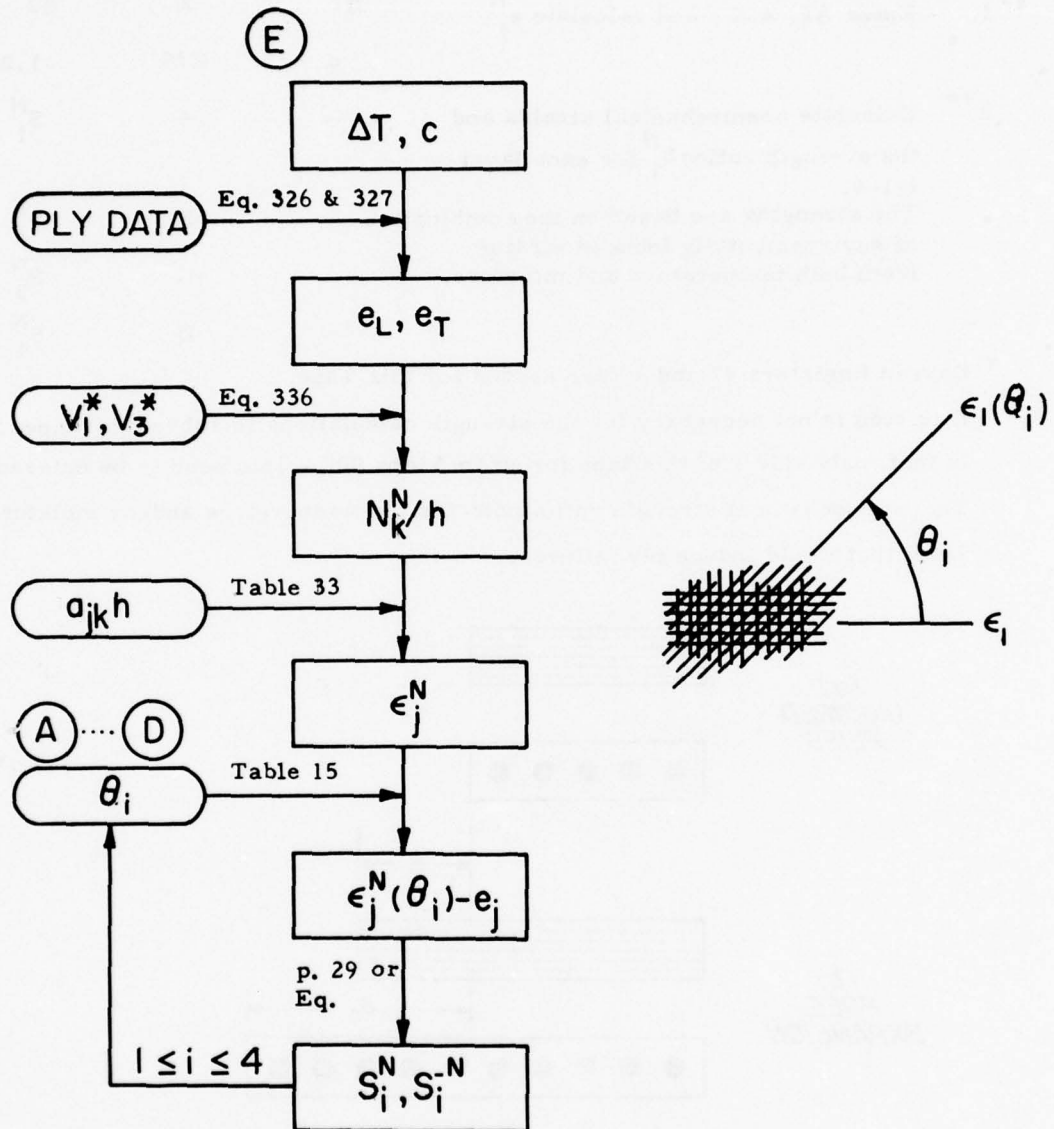
e₃+r

e₄+r

Tape #3 In-Plane Stiffness/Sample Problems

	0.00	00		0.00	00		0.00	00		0.00	00
	181.81114	09	01	181.81114	09	01	181.81114	09	01	181.81114	09
	10.346159	09	02	10.346159	09	02	10.346159	09	02	10.346159	09
	2.8969244	09	03	2.8969244	09	03	2.8969244	09	03	2.8969244	09
	0.00	04		0.00	04		0.00	04		0.00	04
	0.00	05		0.00	05		0.00	05		0.00	05
	0.00	06		0.00	06		0.00	06		0.00	06
	0.00	07		0.00	07		0.00	07		0.00	07
	0.00	08		0.00	08		0.00	08		0.00	08
	0.00	09		0.00	09		0.00	09		0.00	09
	0.00	10		0.00	10		0.00	10		0.00	10
	0.00	11		0.00	11		0.00	11		0.00	11
	0.00	12		0.00	12		0.00	12		0.00	12
θ_i	0.00	13		45.00	13		0.00	13		0.00	13
α_i	1.00	14		1.00	14		1.00	14		1.00	14
	90.00	15		-45.00	15		60.00	15		90.00	15
	1.00	16		1.00	16		1.00	16		1.00	16
	68.06	17		68.06	17		-60.00	17		45.00	17
	181.09	18		181.09	18		1.00	18		1.00	18
	10.309	19		10.309	19		10.309	19		-45.00	19
	280.-03	20		280.-03	20		280.-03	20		1.00	20
	7.1709	21		7.1709	21		7.1709	21		7.1709	21
	10.-09	22		10.-09	22		10.-09	22		10.-09	22
	12.5-06	23		12.5-06	23		12.5-06	23		12.5-06	23
	0.00	24		0.00	24		0.00	24		0.00	24
	600.-03	25		600.-03	25		600.-03	25		600.-03	25
	500.-06	26		500.-06	26		750.-06	26		1.-03	26
R	96.078649	27		56.657787	27		76.368218	27		76.368218	27
A_{ij}/h	96.078649	28		56.657787	28		76.368218	28		76.368218	28
	2.8969244	29		42.317787	29		22.607356	29		22.607356	29
	7.1709	30		46.590862	30		26.880431	30		26.880431	30
	0.00	31		0.00	31		0.00	31		0.00	31
	0.00	32		0.00	32		0.00	32		0.00	32
a_{ij}/h	10.417611	33		39.919255	33		14.352198	33		14.352198	33
	10.417611	34		39.919255	34		14.352198	34		14.352198	34
	-314.10757	35		-29.815752	35		-4.2486946	35		-4.2486946	35
	139.47001	36		21.463436	36		37.201784	36		37.201784	36
	0.00	37		0.00	37		0.00	37		0.00	37
	0.00	38		0.00	38		0.00	38		0.00	38
	66.126864	39		66.126864	39		143.0311	39		143.0311	39
	1.00	40		1.00	40		1.00	40		1.00	40
	125.-06	41		125.-06	41		125.-06	41		125.-06	41
	49.487787	42		49.487787	42		49.487787	42		49.487787	42
	26.880431	43		26.880431	43		26.880431	43		26.880431	43
	85.73249	44		85.73249	44		85.73249	44		85.73249	44
	19.710431	45		19.710431	45		19.710431	45		19.710431	45
	2.00	46		2.00	46		3.00	46		4.00	46
	0.00	47		0.00	47		433.33333	47		0.00	47
	1.00	48		-1.00	48		-733.33333	48		0.00	48
	0.00	49		0.00	49		0.00	49		0.00	49
	0.00	50		0.00	50		0.00	50		0.00	50
	-3.3603243	51		-3.3603243	51		-3.3603243	51		-3.3603243	51
	0.00	52		0.00	52		0.00	52		0.00	52
	0.00	53		0.00	53		0.00	53		0.00	53
	12.004384	54		12.004384	54		12.004384	54		12.004384	54
	10.680652	55		10.680652	55		10.680652	55		10.680652	55
	-3.0691032	56		-3.0691032	56		-3.0691032	56		-3.0691032	56
	11.117842	57		11.117842	57		11.117842	57		11.117842	57
	60.646995	58		60.646995	58		60.646995	58		60.646995	58
	216.59641	59		216.59641	59		216.59641	59		216.59641	59

TAPE #4
IN-PLANE NON MECHANICAL STRAINS
OF SYMMETRIC LAMINATES



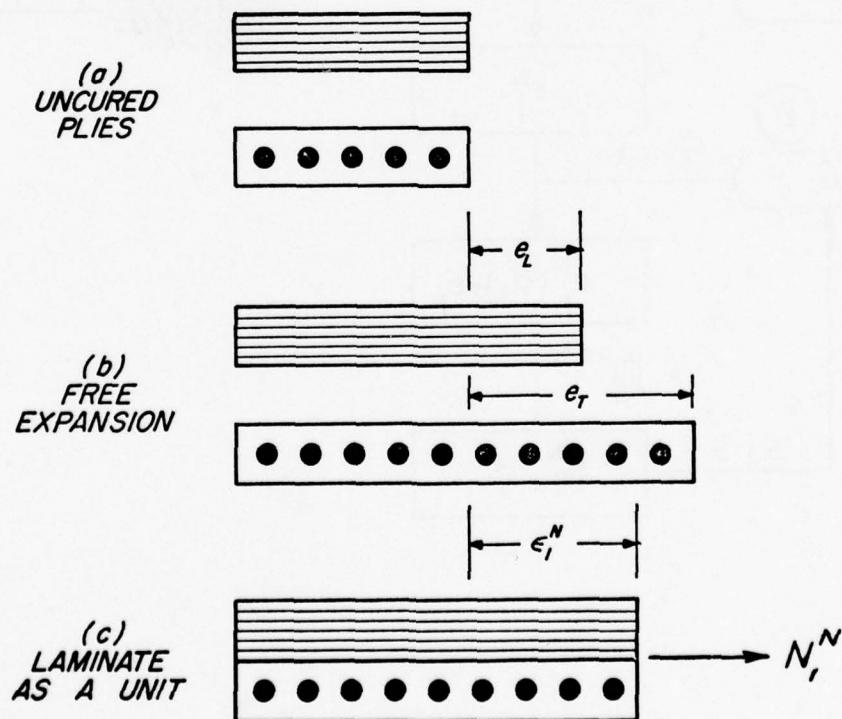
USER INSTRUCTIONS

TAPE #4: IN-PLANE NONMECHANICAL STRAINS OF SYMMETRIC LAMINATES

STEP	PROCEDURE	ENTER	PRESS	DISPLAY
0	Data from Tape #3 must be in storage.*	--		--
1	Enter ΔT , and c and calculate ϵ_j^N	ΔT	E	ΔT
		c	R/S	1.00
2 **	Calculate nonmechanical strains and the strength ratios S_i^N for each layer, $i=1-4$.	--	A	S_1^N
	The strengths are based on the combination of environmentally induced strains from both temperature and moisture.	--	B	S_2^N
		--	C	S_3^N
		--	D	S_4^N

* Data in Registers 47 and 49 are needed for this Tape.

** This step is not necessary for the strength calculations in subsequent tapes. In fact, only side 1 of this tape (program steps 000 - 166) need to be entered. The nonmechanical strength ratio indicates the temperature and/or moisture level that would induce ply failures.



Tape* 4

Title IN-PLANE NONMECHANICAL STRAINS OF SYMMETRIC LAMINATES

KEYS	STORAGE MEMORIES		
A S_1^N	0 γ	20 n_4	40 $q, \dots S_i^N, S_4^N$
	1 Q_{11}	21 $2\theta_i$	41
A'	2 Q_{22}	22 α_L^T	42 I_{1Q}
	3 Q_{12}	23 α_T^T	43 I_{2Q}
B S_2^N	4 N_1^N/h	24 α_L^H	44 R_{1Q}
	5 N_2^N/h	25 α_T^H	45 R_{2Q}
B'	6 N_6^N/h	26 h	46 n
	7 $e_1^N(\theta_i) - e_L$	27 S_1^{-N}	47 v_{1A}^*
C S_3^N	8 $e_2^N(\theta_i) - e_T$	28 S_2^{-N}	48 $v_{2A}^*, \Delta T$
	9 $e_6^N(\theta_i)$	29 S_3^{-N}	49 v_{3A}^*
C'	10 e_1^N	30 S_1^N	50 v_{4A}^*, c
	11 e_2^N	31 S_2^N	51
D S_4^N	12 e_6^N	32 S_3^N	52 e_L
	13 θ_1	33 a_{11}^h	53 e_T
D'	14 n_1	34 a_{22}^h	54 G_{11}
	15 θ_2	35 a_{12}^h	55 G_{22}
E $\Delta T, c$	16 n_2	36 a_{66}^h	56 G_{12}
	17 θ_3	37 a_{16}^h	57 G_{66}
E'	18 n_3	38 a_{26}^h	58 G_1
	19 θ_4	39 $p, A \dots S_4^{-N}$	59 G_2

Tape #4 In-Plane Nonmechanical

N/R

000	76	LRL
001	15	E
002	57	ENG
003	42	STD
004	48	48
005	91	R/S
006	42	STD
007	50	50
008	65	x
009	43	RCL
010	24	24
011	85	+
012	43	RCL
013	48	48
014	65	x
015	43	RCL
016	22	22
017	95	=
018	42	STD
019	52	52
020	08	8
021	66	PAU
022	43	RCL
023	48	48
024	65	x
025	43	RCL
026	23	23
027	85	+
028	43	RCL
029	50	50
030	65	x
031	43	RCL
032	25	25
033	95	=
034	42	STD
035	53	53
036	65	x
037	43	RCL
038	03	03
039	85	+
040	43	RCL
041	52	52
042	65	x
043	43	RCL
044	01	01
045	95	=
046	42	STD
047	39	39
048	43	RCL
049	52	52
050	65	x
051	43	RCL
052	03	03
053	85	+
054	43	RCL
055	53	53
056	65	x
057	43	RCL
058	02	02
059	95	=
060	42	STD
061	40	40
062	85	+
063	43	RCL
064	39	39
065	95	=
066	55	+
067	02	2
068	95	=
069	42	STD
070	39	39
071	75	-
072	43	RCL
073	40	40
074	95	=
075	42	STD
076	40	40
077	65	x
078	43	RCL
079	47	47

080	85	+
081	43	RCL
082	39	39
083	95	=
084	42	STD
085	04	04
086	75	-
087	02	2
088	65	x
089	43	RCL
090	47	47
091	65	x
092	43	RCL
093	40	40
094	95	=
095	42	STD
096	05	05
097	43	RCL
098	49	49
099	65	x
100	43	RCL
101	40	40
102	95	=
103	94	+/-
104	42	STD
105	06	06

ϵ_j^N

106	65	x
107	43	RCL
108	37	37
109	85	+
110	43	RCL
111	04	04
112	65	x
113	43	RCL
114	33	33
115	85	+
116	43	RCL
117	05	05
118	65	x
119	43	RCL
120	35	35
121	95	=
122	42	STD
123	10	10
124	43	RCL
125	04	04
126	65	x
127	43	RCL
128	35	35
129	85	+
130	43	RCL
131	05	05
132	65	x
133	43	RCL
134	34	34
135	85	+
136	43	RCL
137	06	06
138	65	x
139	43	RCL
140	38	38
141	95	=
142	42	STD
143	11	11
144	43	RCL
145	04	04
146	65	x
147	43	RCL
148	37	37
149	85	+
150	43	RCL
151	05	05
152	65	x
153	43	RCL
154	38	38
155	85	+
156	43	RCL
157	06	06
158	65	x
159	43	RCL

160	36	36
161	95	=
162	42	STD
163	12	12
164	01	1
165	95	=
166	91	R/S

S_1^N

167	76	LBL
168	11	A
169	43	RCL
170	13	13
171	71	SBR
172	35	1/X
173	42	STD
174	27	27
175	43	RCL
176	40	40
177	42	STD
178	42	42
179	91	R/S

S_2^N

180	76	LBL
181	12	B
182	43	RCL
183	15	15
184	71	SBR
185	35	1/X
186	42	STD
187	28	28
188	43	RCL
189	40	40
190	42	STD
191	43	43
192	91	R/S

S_3^N

193	76	LBL
194	13	C
195	43	RCL
196	17	17
197	71	SBR
198	35	1/X
199	42	STD
200	29	29
201	43	RCL
202	40	40
203	42	STD
204	44	44
205	91	R/S

S_4^N

206	76	LBL
207	14	D
208	43	RCL
209	19	19
210	71	SBR
211	35	1/X
212	42	STD
213	30	30
214	43	RCL
215	40	40
216	42	STD
217	45	45
218	91	R/S

$\epsilon_j^N(\theta_j) - e_j$

219	76	LBL
220	35	1/X
221	65	x
222	02	2
223	95	=
224	42	STD
225	21	21
226	01	1
227	00	0
228	66	PAU
229	43	RCL
230	10	10
231	85	+
232	43	RCL
233	11	11
234	95	=
235	55	+
236	02	2
237	95	=
238	42	STD
239	39	39

Tape #4 In-Plane Nonmechanical

240	75		320	65	x	400	00	0
241	43	RCL	321	43	RCL	401	00	0
242	11	11	322	07	07	402	00	0
243	95	=	323	65	x	403	00	0
244	42	STD	324	43	RCL	404	00	0
245	40	40	325	08	08	405	00	0
246	65	x	326	85	+	406	00	0
247	43	RCL	327	43	RCL	407	00	0
248	21	21	328	55	55	408	00	0
249	39	CDS	329	65	x	409	00	0
250	85	+	330	43	RCL	410	00	0
251	43	RCL	331	08	08	411	00	0
252	39	39	332	33	X ²	412	00	0
253	85	+	333	95	=	413	00	0
254	53	(334	42	STD	414	00	0
255	43	RCL	335	39	39	415	00	0
256	12	12	336	43	RCL	416	00	0
257	65	x	337	58	58	417	00	0
258	43	RCL	338	65	x	418	00	0
259	21	21	339	43	RCL	419	00	0
260	38	SIN	340	07	07	420	00	0
261	54)	341	85	+	421	00	0
262	55	+	342	43	RCL	422	00	0
263	02	2	343	59	59	423	00	0
264	75	-	344	65	x	424	00	0
265	43	RCL	345	43	RCL	425	00	0
266	52	52	346	08	08	426	00	0
267	95	=	347	95	=	427	00	0
268	42	STD	348	55	+	428	00	0
269	07	07	349	43	RCL	429	00	0
270	75	-	350	39	39	430	00	0
271	43	RCL	351	55	+	431	00	0
272	10	10	352	02	2	432	00	0
273	75	-	353	95	=	433	00	0
274	43	RCL	354	42	STD	434	00	0
275	11	11	355	40	40	435	00	0
276	85	+	356	33	X ²	436	00	0
277	43	RCL	357	85	+	437	00	0
278	52	52	358	43	RCL	438	00	0
279	85	+	359	39	39	439	00	0
280	43	RCL	360	35	1/X	440	00	0
281	53	53	361	95	=	441	00	0
282	95	=	362	34	FX	442	00	0
283	94	+/-	363	42	STD	443	00	0
284	42	STD	364	39	39	444	00	0
285	08	08	365	75	-	445	00	0
286	43	RCL	366	43	RCL	446	00	0
287	12	12	367	40	40	447	00	0
288	65	x	368	95	=	448	00	0
289	43	RCL	369	42	STD	449	00	0
290	21	21	370	40	40	450	00	0
291	39	CDS	371	75	-	451	00	0
292	75	-	372	02	2	452	00	0
293	43	RCL	373	65	x	453	00	0
294	40	40	374	43	RCL	454	00	0
295	65	x	375	39	CDS	455	00	0
296	02	2	376	95	=	456	00	0
297	65	x	377	94	+/-	457	00	0
298	43	RCL	378	92	RTN	458	00	0
299	21	21	379	00	0	459	00	0
300	38	SIN	380	00	0	460	00	0
301	95	=	381	00	0	461	00	0
302	42	STD	382	00	0	462	00	0
303	09	09	383	00	0	463	00	0
304	33	X ²	384	00	0	464	00	0
305	65	x	385	00	0	465	00	0
306	43	RCL	386	00	0	466	00	0
307	57	57	387	00	0	467	00	0
308	85	+	388	00	0	468	00	0
309	43	RCL	389	00	0	469	00	0
310	54	54	390	00	0	470	00	0
311	65	x	391	00	0	471	00	0
312	43	RCL	392	00	0	472	00	0
313	07	07	393	00	0	473	00	0
314	33	X ²	394	00	0	474	00	0
315	85	+	395	00	0	475	00	0
316	02	2	396	00	0	476	00	0
317	65	x	397	00	0	477	00	0
318	43	RCL	398	00	0	478	00	0
319	56	56	399	00	0	479	00	0

Tape #4 In-Plane Nonmechanical / sample problems

0. 00	00	0. 00	00	0. 00	00
181.81114 09	01	181.81114 09	01	181.81114 09	01
10.346159 09	02	10.346159 09	02	10.346159 09	02
2.8969244 09	03	2.8969244 09	03	2.8969244 09	03
-12.553922 06	04	19.864625 06	04	7.3107032 06	04
-12.553922 06	05	19.864625 06	05	7.3107032 06	05
0. 00	06	0. 00	06	0. 00	06
-125.33858-06	07	200.7023-06	07	75.363712-06	07
1.7481614-03	08	-2.7992977-03	08	-1.0511363-03	08
0. 00	09	0. 00	09	0. 00	09
-126.83858-06	10	200.7023-06	10	73.863712-06	10
-126.83858-06	11	200.7023-06	11	73.863712-06	11
0. 00	12	0. 00	12	0. 00	12
0. 00	13	0. 00	13	0. 00	13
1. 00	14	1. 00	14	1. 00	14
90. 00	15	90. 00	15	90. 00	15
1. 00	16	1. 00	16	1. 00	16
68. 06	17	68. 06	17	68. 06	17
181. 09	18	181. 09	18	181. 09	18
10.3 09	19	10.3 09	19	10.3 09	19
280. -03	20	280. -03	20	280. -03	20
180. 00	21	180. 00	21	180. 00	21
10. -09	22	10. -09	22	10. -09	22
12.5-06	23	12.5-06	23	12.5-06	23
0. 00	24	0. 00	24	0. 00	24
600. -03	25	600. -03	25	600. -03	25
500. -06	26	500. -06	26	500. -06	26
13.092402 00	27	1.395767 00	27	3.7170891 00	27
13.092402 00	28	1.395767 00	28	3.7170891 00	28
2.8969244 09	29	2.8969244 09	29	2.8969244 09	29
2.2350152 00	30	8.1762053 00	30	21.774182 00	30
2.2350152 00	31	8.1762053 00	31	21.774182 00	31
0. 00	32	0. 00	32	0. 00	32
10.417611-12	33	10.417611-12	33	10.417611-12	33
10.417611-12	34	10.417611-12	34	10.417611-12	34
-314.10757-15	35	-314.10757-15	35	-314.10757-15	35
139.47001-12	36	139.47001-12	36	139.47001-12	36
0. 00	37	0. 00	37	0. 00	37
0. 00	38	0. 00	38	0. 00	38
7.6637088 00	39	4.7859861 00	39	12.745636 00	39
2.2350152 00	40	8.1762053 00	40	21.774182 00	40
125. -06	41	125. -06	41	125. -06	41
49.487787 09	42	49.487787 09	42	49.487787 09	42
26.880431 09	43	26.880431 09	43	26.880431 09	43
85.73249 09	44	85.73249 09	44	85.73249 09	44
19.710431 09	45	19.710431 09	45	19.710431 09	45
2. 00	46	2. 00	46	2. 00	46
0. 00	47	0. 00	47	0. 00	47
ΔT -150. 00	48	0. 00	48	-150. 00	48
0. 00	49	0. 00	49	0. 00	49
c 0. 00	50	5. -03	50	5. -03	50
-3.3603243-18	51	-3.3603243-18	51	-3.3603243-18	51
-1.5-06	52	0. 00	52	-1.5-06	52
-1.875-03	53	3. -03	53	1.125-03	53
12.004384 03	54	12.004384 03	54	12.004384 03	54
10.680652 03	55	10.680652 03	55	10.680652 03	55
-3.0691032 03	56	-3.0691032 03	56	-3.0691032 03	56
11.117842 03	57	11.117842 03	57	11.117842 03	57
60.646995 00	58	60.646995 00	58	60.646995 00	58
216.59641 00	59	216.59641 00	59	216.59641 00	59

TAPE #4

STRENGTH RATIOS FOR NONMECHANICAL STRAINS OF LAMINATES

Define $S^N = \left[\frac{e_{\text{allowed}}}{e_{\text{imposed}}} \right]^N$

The strains that must satisfy the failure criterion are

$$e_i^N \Big|_{\text{allowed}} = \left[e_i^N - e_i \right]_{\text{all.}} = \begin{Bmatrix} e_1^N - e_L \\ e_2^N - e_T \\ e_6^N \end{Bmatrix}_{\text{allowed}}$$

where e_i^N = nonmechanical strains

$e_i = \{e_L, e_T, 0\}$ = longitudinal, and transverse strains induced by temperature and moisture.

Final failure criterion

$$G_{ij}(e_i^N - e_i)(e_j^N - e_j) + G_i(e_i^N - e_i) = 1$$

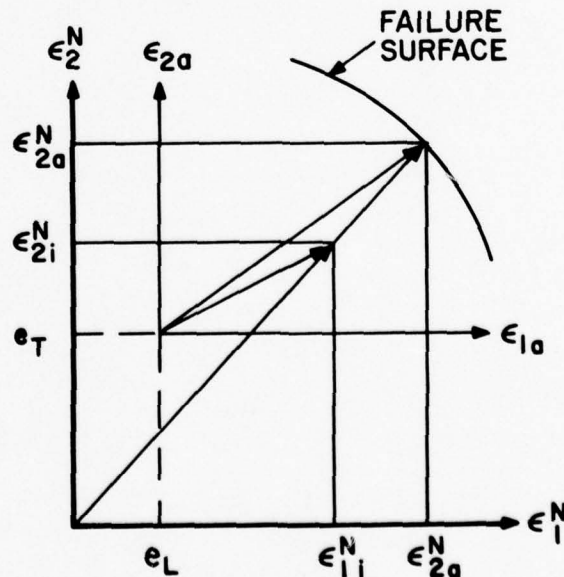
In terms of strength ratio S^N and imposed strain (nonmechanical):

$$G_{ij} S^N (e_i^N - e_i) S^N (e_j^N - e_j) + G_i S^N (e_i^N - e_i) = 1$$

Expand this equation and solve for S^N :

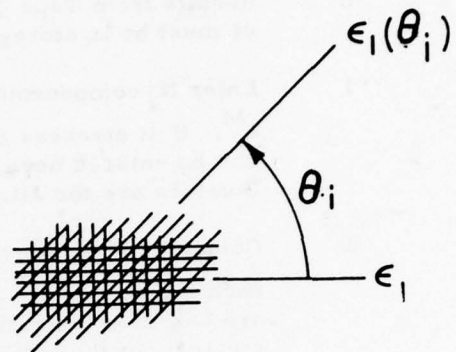
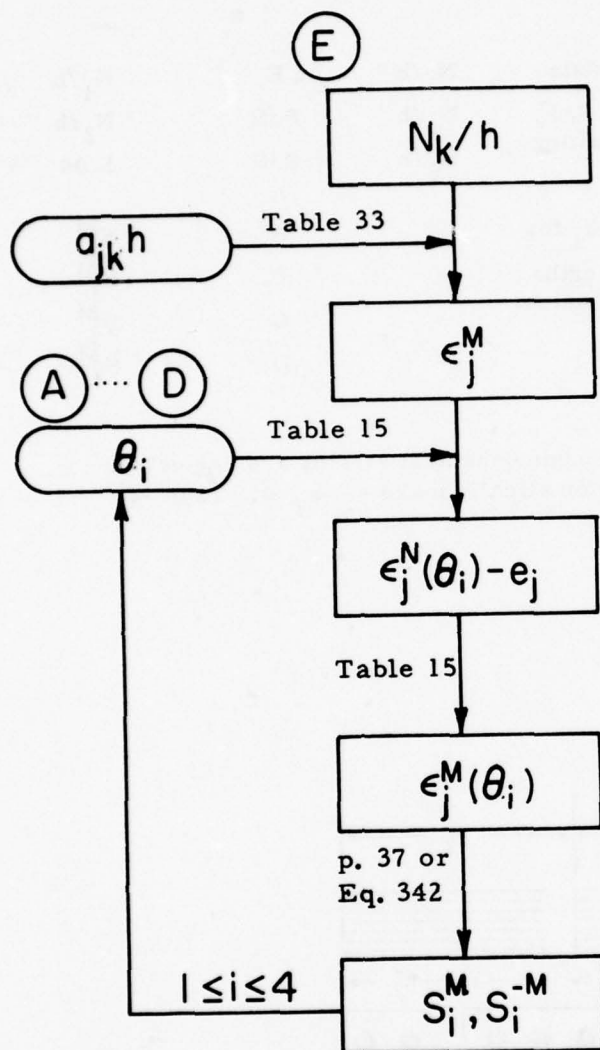
$$a(S^N)^2 + bS^N + c = 0$$

The two roots are S^N and S^{-N} .



TAPE #5

IN-PLANE STRENGTH OF SYMMETRIC LAMINATES



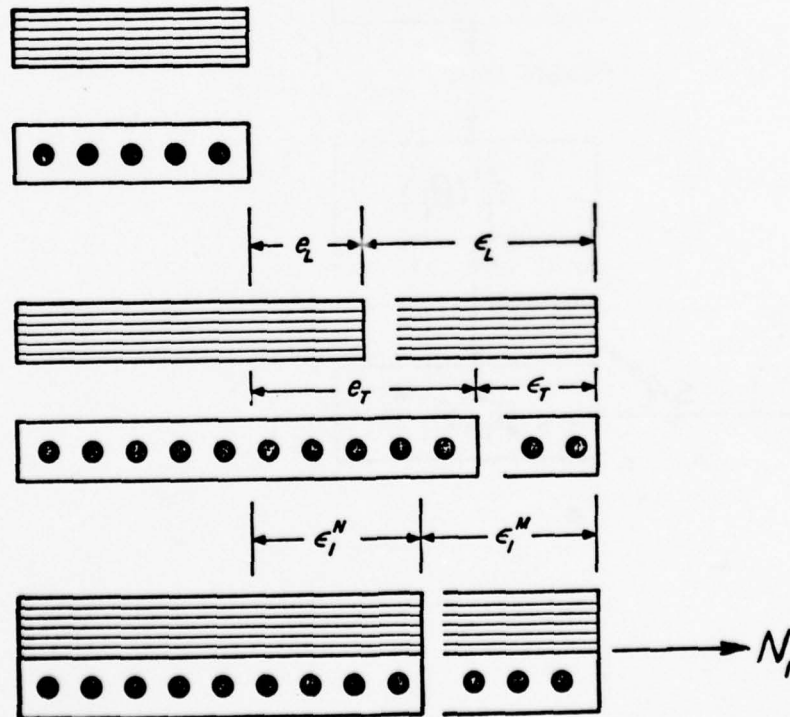
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USER INSTRUCTIONS

TAPE #5: IN-PLANE STRENGTH OF SYMMETRIC LAMINATES

STEP	PROCEDURE	ENTER	PRESS	DISPLAY
0	Results from Tape #3, c = #3 and #4 must be in storage*	--		--
1	Enter N_k components and calculate e_i^M . Unit stresses such as [1,0,0] can be entered here. The resulting S values are the allowables.	N_1/h N_2/h N_6/h	E R/S R/S	N_1/h N_2/h 1.00
2	Calculate strength ratios S_i & S_i^M for each layer, $i=1-4$. These strengths are based on the ratios of mechanical strains; not the total strains.	-- -- -- --	A B C D	S_1^M S_2^M S_3^M S_4^M

*Tape #5 can be used following Tape #3 if nonmechanical strains are neglected. Ply data tape used in Step 0 of Tape #3 automatically make $e_L = e_T = 0$. Tape #4 need not be run for making $\Delta T = c = 0$.



Tape# 5

Title IN-PLANE STRENGTH OF SYMMETRIC LAMINATES

KEYS	STORAGE MEMORIES		
A S_1^M	0	20	40
	1 N_1/h	21 $2\theta_i$	41
A'	2 N_2/h	22	42 S_1^M
	3 N_6/h	23	43 S_2^M
B S_2^M	4	24	44 S_3^M
	5	25	45 S_4^M
B'	6	26	46
	7 ϵ_1^M	27 $\epsilon_1^M(\theta_i)$	47 S_1^M
C S_3^M	8 ϵ_2^M	28 $\epsilon_2^M(\theta_i)$	48 S_2^M
	9 ϵ_6^M	29 $\epsilon_6^M(\theta_i)$	49 S_3^M
C'	10 ϵ_1^N	30 $\epsilon_1^N(\theta_i) - e_L$	50 S_4^M
	11 ϵ_2^N	31 $\epsilon_2^N(\theta_i) - e_T$	51
D S_4^M	12 ϵ_6^N	32 $\epsilon_6^N(\theta_i)$	52 e_L
	13 θ_1	33 a_{11}^h	53 e_T
D'	14	34 a_{22}^h	54 G_{11}
	15 θ_2	35 a_{12}^h	55 G_{22}
E $N_k/h, \epsilon_j^M$	16	36 a_{66}^h	56 G_{12}
	17 θ_3	37 a_{16}^h	57 G_{66}
E'	18	38 a_{26}^h	58 G_1
	19 θ_4	39	59 G_2

Tape #5 In-Plane Strength

N_x/r 000 76 LBL
 001 15 E
 002 42 STD
 003 01 01
 004 91 R/S
 005 42 STD
 006 02 02
 007 91 R/S
 008 42 STD
 009 03 03

 ϵ_j^m 010 65 x
 011 43 RCL
 012 37 37
 013 85 +
 014 43 RCL
 015 01 01
 016 65 x
 017 43 RCL
 018 33 33
 019 85 +
 020 43 RCL
 021 02 02
 022 65 x
 023 43 RCL
 024 35 35
 025 95 =
 026 42 STD
 027 07 07
 028 43 RCL
 029 01 01
 030 65 x
 031 43 RCL
 032 35 35
 033 85 +
 034 43 RCL
 035 02 02
 036 65 x
 037 43 RCL
 038 34 34
 039 85 +
 040 43 RCL
 041 03 03
 042 65 x
 043 43 RCL
 044 38 38
 045 95 =
 046 42 STD
 047 08 08
 048 43 RCL
 049 01 01
 050 65 x
 051 43 RCL
 052 37 37
 053 85 +
 054 43 RCL
 055 02 02
 056 65 x
 057 43 RCL
 058 38 38
 059 85 +
 060 43 RCL
 061 03 03
 062 65 x
 063 43 RCL
 064 36 36
 065 95 =
 066 42 STD
 067 09 09
 068 01 1
 069 95 =
 070 91 R/S

 ϵ_j^m 071 76 LBL
 072 11 A
 073 43 RCL
 074 13 13
 075 71 SBR
 076 35 1/X
 077 42 STD
 078 47 47
 079 43 RCL

080 40 40
 081 42 STD
 082 42 42
 083 91 R/S

 S_2^m 084 76 LBL
 085 12 B
 086 43 RCL
 087 15 15
 088 71 SBR
 089 35 1/X
 090 42 STD
 091 48 48
 092 43 RCL
 093 40 40
 094 42 STD
 095 43 43

 S_3^m 096 91 R/S
 097 76 LBL
 098 13 C
 099 43 RCL
 100 17 17
 101 71 SBR
 102 35 1/X
 103 42 STD
 104 49 49
 105 43 RCL
 106 40 40
 107 42 STD
 108 44 44
 109 91 R/S

 S_4^m 110 76 LBL
 111 14 D
 112 43 RCL
 113 19 19
 114 71 SBR
 115 35 1/X
 116 42 STD
 117 50 50
 118 43 RCL
 119 40 40
 120 42 STD
 121 45 45
 122 91 R/S

 $\epsilon_j^N(\theta_i)$ 123 76 LBL
 124 35 1/X
 125 65 x
 126 02 2
 127 95 =
 128 42 STD
 129 21 21
 130 01 1
 131 08 8
 132 66 PAU
 133 43 RCL
 134 10 10
 135 85 +
 136 43 RCL
 137 11 11
 138 95 =
 139 55 +
 140 02 2
 141 5 =
 142 42 STD
 143 39 39
 144 75 -
 145 43 RCL
 146 11 11
 147 95 =
 148 42 STD
 149 40 40
 150 65 x
 151 43 RCL
 152 21 21
 153 39 CDS
 154 85 +
 155 43 RCL
 156 39 39
 157 85 +
 158 43 RCL
 159 12 12

160 65 x
 161 43 RCL
 162 21 21
 163 38 SIN
 164 55 +
 165 02 2
 166 75 -
 167 43 RCL
 168 52 52
 169 95 =
 170 42 STD
 171 30 30
 172 75 -
 173 43 RCL
 174 10 10
 175 75 -
 176 43 RCL
 177 11 11
 178 85 +
 179 43 RCL
 180 52 52
 181 85 +
 182 43 RCL
 183 53 53
 184 95 =
 185 94 +/-
 186 42 STD
 187 31 31
 188 43 RCL
 189 12 12
 190 65 x
 191 43 RCL
 192 21 21
 193 39 CDS
 194 75 -
 195 43 RCL
 196 40 40
 197 65 x
 198 02 2
 199 65 x
 200 43 RCL
 201 21 21
 202 38 SIN
 203 95 =
 204 42 STD
 205 32 32

 $\epsilon_j^m(\theta_i)$ 206 43 RCL
 207 07 07
 208 85 +
 209 43 RCL
 210 08 08
 211 95 =
 212 55 +
 213 02 2
 214 95 =
 215 42 STD
 216 39 39
 217 75 -
 218 43 RCL
 219 08 08
 220 95 =
 221 42 STD
 222 40 40
 223 65 x
 224 43 RCL
 225 21 21
 226 39 CDS
 227 85 +
 228 43 RCL
 229 39 39
 230 85 +
 231 43 RCL
 232 09 09
 233 65 x
 234 43 RCL
 235 21 21
 236 38 SIN
 237 55 +
 238 02 2
 239 95 =

Tape #5 In-Plane Strength

240	42	STD	320	43	RCL	400	32	32	
241	27	27	321	27	27	401	33	X ²	
242	75	-	322	65	x	402	75	-	
243	43	RCL	323	43	RCL	403	43	RCL	
244	07	07	324	30	30	404	58	58	
245	75	-	325	85	+	405	65	x	
246	43	RCL	326	43	RCL	406	43	RCL	
247	08	08	327	56	56	407	30	30	
248	95	=	328	65	x	408	75	-	
249	34	+/-	329	53	<	409	43	RCL	
250	42	STD	330	43	RCL	410	59	59	
251	28	28	331	27	27	411	65	x	
252	43	RCL	332	65	x	412	43	RCL	
253	09	09	333	43	RCL	413	31	31	
254	65	x	334	31	31	414	95	=	
255	43	RCL	335	85	+	415	55	+	
256	21	21	336	43	RCL	416	43	RCL	
257	39	CDS	337	28	28	417	39	39	
258	75	-	338	65	x	418	85	+	
259	43	RCL	339	43	RCL	419	43	RCL	
260	40	40	340	30	30	420	40	40	
261	65	x	341	54	>	421	33	X ²	
262	02	2	342	85	+	422	95	=	
263	65	x	343	43	RCL	423	34	FX	
264	43	RCL	344	55	55	424	42	STD	
265	21	21	345	65	x	425	39	39	
266	38	SIN	346	43	RCL	426	75	-	
267	95	=	347	28	28	427	43	RCL	
268	42	STD	348	65	x	428	40	40	
269	29	29	349	43	RCL	429	95	=	
S _i ^m	270	33	X ²	350	31	31	430	42	STD
	271	65	x	351	85	+	431	40	40
272	43	RCL	352	43	RCL	432	75	-	
273	57	57	353	57	57	433	02	2	
274	85	+	354	65	x	434	65	x	
275	43	RCL	355	43	RCL	435	43	RCL	
276	54	54	356	29	29	436	39	39	
277	65	x	357	65	x	437	95	=	
278	43	RCL	358	43	RCL	438	94	+/-	
279	27	27	359	32	32	439	92	RTN	
280	33	X ²	360	95	=	440	00	0	
281	85	+	361	55	+	441	00	0	
282	02	2	362	43	RCL	442	00	0	
283	65	x	363	39	39	443	00	0	
284	43	RCL	364	55	+	444	00	0	
285	56	56	365	02	2	445	00	0	
286	65	x	366	95	=	446	00	0	
287	43	RCL	367	42	STD	447	00	0	
288	27	27	368	40	40	448	00	0	
289	65	x	369	01	1	449	00	0	
290	43	RCL	370	75	-	450	00	0	
291	28	28	371	43	RCL	451	00	0	
292	85	+	372	54	54	452	00	0	
293	43	RCL	373	65	x	453	00	0	
294	55	55	374	43	RCL	454	00	0	
295	65	x	375	30	30	455	00	0	
296	43	RCL	376	33	X ²	456	00	0	
297	28	28	377	75	-	457	00	0	
298	33	X ²	378	02	2	458	00	0	
299	95	=	379	65	x	459	00	0	
300	42	STD	380	43	RCL	460	00	0	
301	39	39	381	56	56	461	00	0	
302	43	RCL	382	65	x	462	00	0	
303	58	58	383	43	RCL	463	00	0	
304	65	x	384	30	30	464	00	0	
305	43	RCL	385	65	x	465	00	0	
306	27	27	386	43	RCL	466	00	0	
307	85	+	387	31	31	467	00	0	
308	43	RCL	388	75	-	468	00	0	
309	59	59	389	43	RCL	469	00	0	
310	65	x	390	55	55	470	00	0	
311	43	RCL	391	65	x	471	00	0	
312	28	28	392	43	RCL	472	00	0	
313	85	+	393	31	31	473	00	0	
314	02	2	394	33	X ²	474	00	0	
315	65	x	395	75	-	475	00	0	
316	53	<	396	43	RCL	476	00	0	
317	43	RCL	397	57	57	477	00	0	
318	54	54	398	65	x	478	00	0	
319	65	x	399	43	RCL	479	00	0	

Tape #5 In-Plane Strength/Sample Problems

	0. 00	0. 00	00	0. 00	0. 00	00
N_k	1. 00	1. 00	01	1. 00	1. 00	01
	0. 00	0. 00	02	0. 00	0. 00	02
	0. 00	0. 00	03	0. 00	0. 00	03
	7.3107032 06	0. 00	04	-111.69921 00	0. 00	04
	7.3107032 06	0. 00	05	111.69921 00	0. 00	05
	0. 00	0. 00	06	0. 00	0. 00	06
	10.417611-12	10.417611-12	07	39.919255-12	39.919255-12	07
	-314.10757-15	-314.10757-15	08	-29.815752-12	-29.815752-12	08
	0. 00	0. 00	09	0. 00	0. 00	09
	73.863712-06	0. 00	10	-7.7893455-09	0. 00	10
	73.863712-06	0. 00	11	7.7893455-09	0. 00	11
	0. 00	0. 00	12	0. 00	0. 00	12
θ_i	0. 00	0. 00	13	45. 00	45. 00	13
n_i	1. 00	1. 00	14	1. 00	1. 00	14
	90. 00	90. 00	15	-45. 00	-45. 00	15
	1. 00	1. 00	16	1. 00	1. 00	16
	68. 06	68. 06	17	68. 06	68. 06	17
	181. 09	181. 09	18	181. 09	181. 09	18
	10.3 09	10.3 09	19	10.3 09	10.3 09	19
	280. -03	280. -03	20	280. -03	280. -03	20
	180. 00	180. 00	21	-90. 00	-90. 00	21
	10. -09	10. -09	22	10. -09	10. -09	22
	12.5-06	12.5-06	23	12.5-06	12.5-06	23
	0. 00	0. 00	24	0. 00	0. 00	24
	600. -03	600. -03	25	600. -03	600. -03	25
	500. -06	500. -06	26	500. -06	500. -06	26
	-314.10757-15	-314.10757-15	27	5.0517515-12	5.0517515-12	27
	10.417611-12	10.417611-12	28	5.0517515-12	5.0517515-12	28
	0. 00	0. 00	29	69.735007-12	69.735007-12	29
	75.363712-06	0. 00	30	1.5-06	0. 00	30
	-1.0511363-03	0. 00	31	-1.125-03	0. 00	31
	0. 00	0. 00	32	-15.578691-09	0. 00	32
	10.417611-12	10.417611-12	33	39.919255-12	39.919255-12	33
	10.417611-12	10.417611-12	34	39.919255-12	39.919255-12	34
	-314.10757-15	-314.10757-15	35	-29.815752-12	-29.815752-12	35
	139.47001-12	139.47001-12	36	21.463436-12	21.463436-12	36
	0. 00	0. 00	37	0. 00	0. 00	37
	0. 00	0. 00	38	0. 00	0. 00	38
	1.3193015 09	1.3211072 09	39	150.73203 06	136.08024 06	39
	473.81212 06	373.39552 06	40	138.67287 06	123.2282 06	40
σ_3	125. -06	125. -06	41	125. -06	125. -06	41
	739.83225 06	681.88201 06	42	138.67287 06	123.2282 06	42
	473.81212 06	373.39552 06	43	138.67287 06	123.2282 06	43
	85.73249 09	85.73249 09	44	85.73249 09	85.73249 09	44
	19.710431 09	19.710431 09	45	19.710431 09	19.710431 09	45
	2. 00	2. 00	46	2. 00	2. 00	46
σ_{-1}	1.2360994 09	1.1077053 09	47	162.79119 06	148.93229 06	47
	2.1647909 09	2.2688189 09	48	162.79119 06	148.93229 06	48
	0. 00	0. 00	49	0. 00	0. 00	49
	5. -03	0. 00	50	5. -03	0. 00	50
	-3.3603243-18	-3.3603243-18	51	-3.3603243-18	-3.3603243-18	51
	-1.5-06	0. 00	52	-1.5-06	0. 00	52
	1.125-03	0. 00	53	1.125-03	0. 00	53
	12.004384 03	12.004384 03	54	12.004384 03	12.004384 03	54
	10.680652 03	10.680652 03	55	10.680652 03	10.680652 03	55
	-3.0691032 03	-3.0691032 03	56	-3.0691032 03	-3.0691032 03	56
	11.117842 03	11.117842 03	57	11.117842 03	11.117842 03	57
	60.646995 00	60.646995 00	58	60.646995 00	60.646995 00	58
	216.59641 00	216.59641 00	59	216.59641 00	216.59641 00	59

STRENGTH RATIOS FOR MECHANICAL STRAINS OF LAMINATES

Define
$$S^M = \frac{e_{\text{allowed}}^M}{e_{\text{imposed}}^M}$$

The strains that must satisfy the failure criterion are:

$$\begin{aligned} e_i]_{\text{allowed}} &= e_i^M]_{\text{allowed}} + e_i^N - e_i \\ &= \begin{pmatrix} e_1^M + e_1^N - e_L \\ e_2^M + e_2^N - e_T \\ e_6^M + e_6^N \end{pmatrix} \end{aligned}$$

Final failure criterion

$$G_{ij}(e_{ia}^M + e_i^N - e_i)(e_{ja}^M + e_j^N - e_j) + G_i(e_{ia}^M + e_i^N - e_i) = 1$$

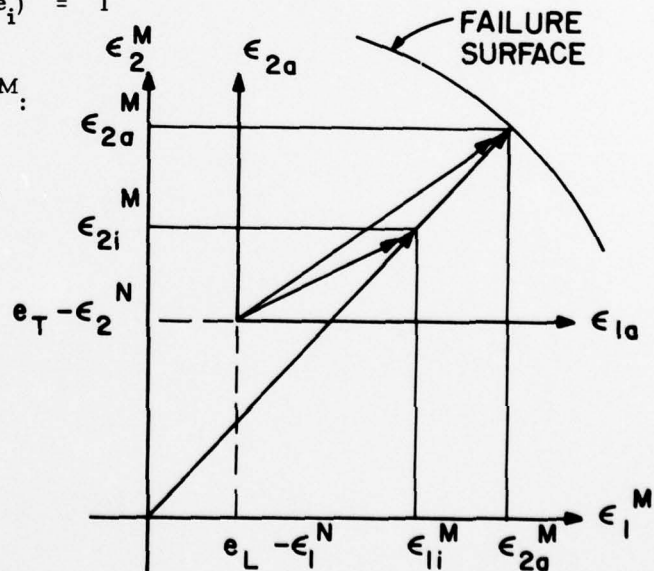
In terms of safety factor S^M , and e_{imposed}^M

$$\begin{aligned} G_{ij}(S^M e_i^M + e_i^N - e_i)(S^M e_j^M + e_j^N - e_j) \\ + G_i(S^M e_i^M + e_i^N - e_i) = 1 \end{aligned}$$

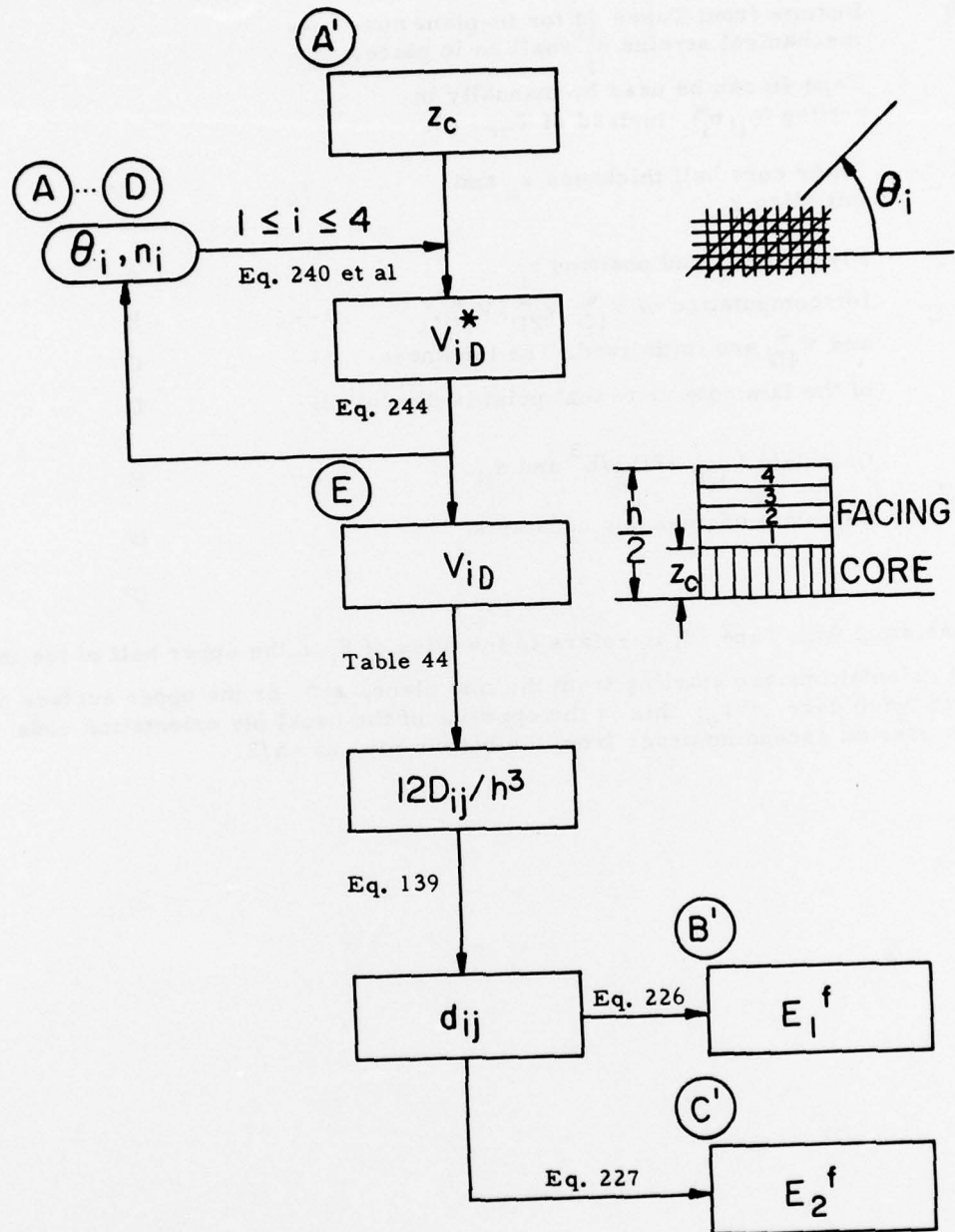
Expand this equation and solve for S^M :

$$a(S^M)^2 + bS^M + c = 0$$

The two roots are S^M and S^{-M} .



TAPE #6
FLEXURAL RIGIDITY OF SYMMETRIC SANDWICH PLATES



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USER INSTRUCTIONS

TAPE #6: FLEXURAL RIGIDITY OF SYMMETRIC SANDWICH PLATES

STEP	PROCEDURE	ENTER	PRESS	DISPLAY
0	Results from Tapes #4 for in-plane non-mechanical strains ϵ_j^N shall be in place. Tape #6 can be used by manually inputting (θ_i, n_i^*) , instead of Tape #3.	--	--	--
1	Enter core half thickness z_c and initialize z_i	z_c	A'	0.00
2	Ply angle θ_i^* and position z_i for computation of $V_{1D}^*, V_{2D}^*, V_{3D}^*$ and V_{4D}^* are initialized. The thickness of the laminate up to that point is displayed.	-- -- --	A B C D	$2z_1$ $2z_2$ $2z_3$ $2z_4$
3	Calculate $V_{iD}, 12D_{ij}/h^3$ and d_{ij} .	--	E	1.00
4	Calculate engineering constants		B' C'	E_1^f E_2^f

* Consistent with Tape #3, n_i refers to the plies of θ_i in the upper half of the laminate.

** Ply orientations are starting from the mid plane, $z=0$, or the upper surface of the sandwich core, $z=z_c$; this is the opposite of the usual ply orientation code which uses an ascending order from the bottom ply, $z=-h/2$.

Tape* 6

FLEXURAL RIGIDITY OF SYMMETRIC SANDWICH PLATES

KEYS	STORAGE MEMORIES		
A θ_1	0	20 $n_4, z_4 = \frac{h}{2}$	40
	1	21 z_c	41 h_o
A' z_c, z_i	2	22 v_{1D}	42 I_{1Q}
	3	23 v_{2D}	43 I_{2Q}
B θ_2	4	24 v_{3D}	44 R_{1Q}
	5	25 v_{4D}	45 R_{2Q}
B' E_1^f	6	26	46 $1 - \left(\frac{2z_c}{h}\right)^3$
	7	27 $12 D_{11}/h^3$	47
C θ_3	8	28 $12 D_{22}/h^3$	48
	9	29 $12 D_{12}/h^3$	49 $2\theta_i$
C' E_2^f	10 e_1^N	30 $12 D_{66}/h^3$	50 $z_i^3 - z_{i-1}^3$
	11 e_2^N	31 $12 D_{16}/h^3$	51 $h/2, h^3/12$
D θ_4	12 e_6^N	32 $12 D_{26}/h^3$	52 e_L
	13 θ_1	33 d_{11}	53 e_T
D'	14 n_1, z_1	34 d_{22}	54 G_{11}
	15 θ_2	35 d_{12}	55 G_{22}
E $12 D_{ij}/h^3, d_{ij}$	16 n_2, z_2	36 d_{66}	56 G_{12}
	17 θ_3	37 d_{16}	57 G_{66}
E'	18 n_3, z_3	38 d_{26}	58 G_1
	19 θ_4	39 $ D $	59 G_2

Tape #6 Flexural Rigidity

β_i
 000 76 LBL
 001 16 R
 002 42 STD
 003 21 21
 004 85 +
 005 43 RCL
 006 14 14
 007 65 x
 008 43 RCL
 009 41 41
 010 95 =
 011 42 STD
 012 14 14
 013 85 +
 014 43 RCL
 015 16 16
 016 65 x
 017 43 RCL
 018 41 41
 019 95 =
 020 42 STD
 021 16 16
 022 85 +
 023 43 RCL
 024 18 18
 025 65 x
 026 43 RCL
 027 41 41
 028 95 =
 029 42 STD
 030 18 18
 031 85 +
 032 43 RCL
 033 20 20
 034 65 x
 035 43 RCL
 036 41 41
 037 95 =
 038 42 STD
 039 20 20
 040 00 0
 041 42 STD
 042 22 22
 043 42 STD
 044 23 23
 045 42 STD
 046 24 24
 047 42 STD
 048 25 25
 049 91 R/S

 β_1
 050 76 LBL
 051 11 R
 052 43 RCL
 053 14 14
 054 42 STD
 055 51 51
 056 45 YX
 057 03 3
 058 75 -
 059 43 RCL
 060 21 21
 061 45 YX
 062 03 3
 063 95 =
 064 42 STD
 065 50 50
 066 43 RCL
 067 13 13
 068 71 SBR
 069 33 X²

 β_2
 070 76 LBL
 071 12 B
 072 43 RCL
 073 16 16
 074 42 STD
 075 51 51
 076 45 YX
 077 03 3
 078 75 -
 079 43 RCL

080 14 14
 081 45 YX
 082 03 3
 083 95 =
 084 42 STD
 085 50 50
 086 43 RCL
 087 15 15
 088 71 SBR
 089 33 X²

 β_3
 090 76 LBL
 091 13 0
 092 43 RCL
 093 18 18
 094 42 STD
 095 51 51
 096 45 YX
 097 03 3
 098 75 -
 099 43 RCL
 100 16 16
 101 45 YX
 102 03 3
 103 95 =
 104 42 STD
 105 50 50
 106 43 RCL
 107 17 17
 108 71 SBR
 109 33 X²

 β_4
 110 76 LBL
 111 14 0
 112 43 RCL
 113 20 20
 114 42 STD
 115 51 51
 116 45 YX
 117 03 3
 118 75 -
 119 43 RCL
 120 18 18
 121 45 YX
 122 03 3
 123 95 =
 124 42 STD
 125 50 50
 126 43 RCL
 127 19 19

 V_{iD}^*
 128 76 LBL
 129 33 X²
 130 65 x
 131 02 2
 132 95 =
 133 94 +/-
 134 42 STD
 135 49 49
 136 39 COS
 137 65 x
 138 43 RCL
 139 50 50
 140 95 =
 141 44 SUM
 142 22 22
 143 43 RCL
 144 49 49
 145 38 SIN
 146 65 x
 147 43 RCL
 148 50 50
 149 95 =
 150 44 SUM
 151 24 24
 152 02 2
 153 49 PRD
 154 49 49
 155 43 RCL
 156 49 49
 157 39 COS
 158 65 x
 159 43 RCL

160 50 50
 161 95 =
 162 44 SUM
 163 23 23
 164 43 RCL
 165 49 49
 166 38 SIN
 167 65 x
 168 43 RCL
 169 50 50
 170 95 =
 171 44 SUM
 172 25 25
 173 43 RCL
 174 51 51
 175 65 x
 176 02 2
 177 95 =
 178 91 R/S

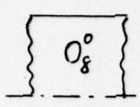
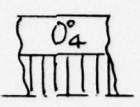
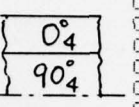
 V_{iD}
 179 76 LBL
 180 15 E
 181 01 1
 182 03 3
 183 66 PRD
 184 43 RCL
 185 51 51
 186 45 YX
 187 03 3
 188 95 =
 189 35 1/X
 190 49 PRD
 191 22 22
 192 49 PRD
 193 23 23
 194 49 PRD
 195 24 24
 196 49 PRD
 197 25 25
 198 65 x
 199 43 RCL
 200 21 21
 201 45 YX
 202 03 3
 203 75 -
 204 01 1
 205 95 =
 206 94 +/-
 207 42 STD
 208 46 46

 $\frac{12}{43} D_{ij}$
 209 43 RCL
 210 42 42
 211 85 +
 212 43 RCL
 213 43 43
 214 95 =
 215 65 x
 216 43 RCL
 217 46 46
 218 85 +
 219 43 RCL
 220 22 22
 221 65 x
 222 43 RCL
 223 44 44
 224 85 +
 225 43 RCL
 226 23 23
 227 65 x
 228 43 RCL
 229 45 45
 230 95 =
 231 42 STD
 232 27 27
 233 75 -
 234 02 2
 235 65 x
 236 43 RCL
 237 22 22
 238 65 x
 239 43 RCL

Tape #6 Flexural Rigidity

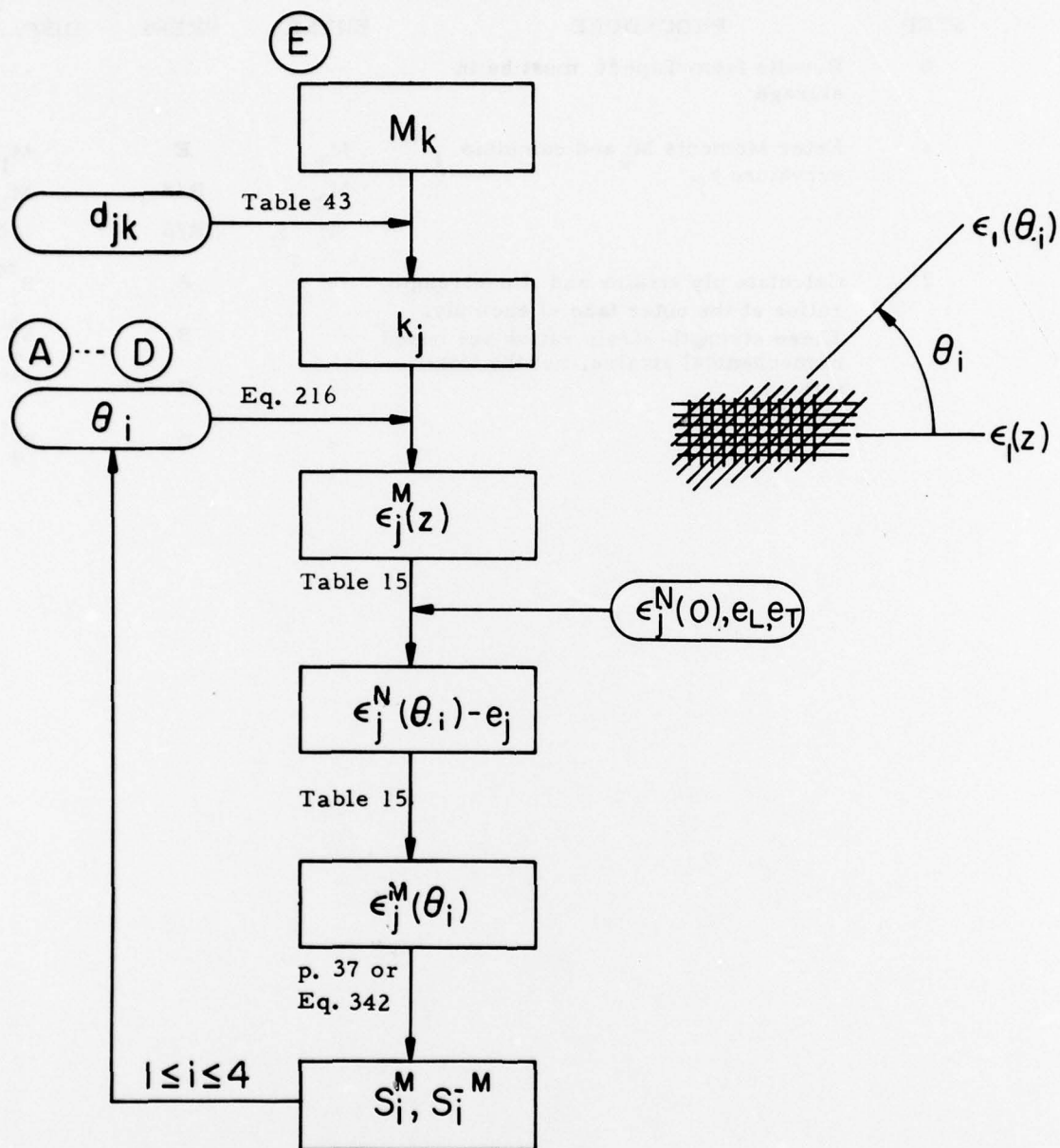
240	44	44	320	31	31	400	43	RCL
241	95	=	321	65	x	401	31	31
242	42	STD	322	43	RCL	402	65	x
243	28	28	323	32	32	403	43	RCL
244	43	RCL	324	65	x	404	32	32
245	42	42	325	02	2	405	75	-
246	75	-	326	75	-	406	43	RCL
247	43	RCL	327	43	RCL	407	29	29
248	43	43	328	28	28	408	65	x
249	95	=	329	65	x	409	43	RCL
250	65	x	330	43	RCL	410	30	30
251	43	RCL	331	31	31	411	95	=
252	46	46	332	33	X ²	412	42	STD
253	75	-	333	75	-	413	35	35
254	43	RCL	334	43	RCL	414	43	RCL
255	23	23	335	27	27	415	29	29
256	65	x	336	65	x	416	65	x
257	43	RCL	337	43	RCL	417	43	RCL
258	45	45	338	32	32	418	31	31
259	95	=	339	33	X ²	419	75	-
260	42	STD	340	75	-	420	43	RCL
261	29	29	341	43	RCL	421	27	27
262	75	-	342	30	30	422	65	x
263	43	RCL	343	65	x	423	43	RCL
264	42	42	344	43	RCL	424	32	32
265	65	x	345	29	29	425	95	=
266	43	RCL	346	33	X ²	426	42	STD
267	46	46	347	95	=	427	38	38
268	85	+	348	42	STD	428	43	RCL
269	02	2	349	39	39	429	51	51
270	65	x	350	43	RCL	430	45	YX
271	43	RCL	351	28	28	431	03	3
272	43	43	352	65	x	432	65	x
273	65	x	353	43	RCL	433	02	2
274	43	RCL	354	30	30	434	55	-
275	46	46	355	75	-	435	03	3
276	95	=	356	43	RCL	436	95	=
277	42	STD	357	32	32	437	42	STD
278	30	30	358	33	X ²	438	51	51
279	43	RCL	359	95	=	439	65	x
280	24	24	360	42	STD	440	43	RCL
281	65	x	361	33	33	441	39	39
282	43	RCL	362	43	RCL	442	95	=
283	44	44	363	27	27	443	35	1/X
284	55	+	364	65	x	444	49	PRD
285	02	2	365	43	RCL	445	33	33
286	85	+	366	28	28	446	49	PRD
287	43	RCL	367	75	-	447	34	34
288	25	25	368	43	RCL	448	49	PRD
289	65	x	369	29	29	449	35	35
290	43	RCL	370	33	X ²	450	49	PRD
291	45	45	371	95	=	451	36	36
292	95	=	372	42	STD	452	99	PRD
293	94	+/-	373	36	36	453	37	37
294	42	STD	374	43	RCL	454	49	PRD
295	31	31	375	27	27	455	38	38
296	85	+	376	65	x	456	01	1
297	02	2	377	43	RCL	457	95	=
298	65	x	378	30	30	458	91	R/S
299	43	RCL	379	75	-	459	76	LBL
300	25	25	380	43	RCL	460	17	B'
301	65	x	381	31	31	461	43	RCL
302	43	RCL	382	33	X ²	462	33	33
303	45	45	383	95	=	463	65	x
304	95	=	384	42	STD	464	43	RCL
305	42	STD	385	34	34	465	51	51
306	32	32	386	43	RCL	466	95	=
307	43	RCL	387	29	29	467	35	1/X
308	27	27	388	65	x	468	91	R/S
309	65	x	389	43	RCL	469	76	LBL
310	43	RCL	390	32	32	470	18	C'
311	28	28	391	75	-	471	43	RCL
312	65	x	392	43	RCL	472	34	34
313	43	RCL	393	28	28	473	65	x
314	30	30	394	65	x	474	43	RCL
315	85	+	395	43	RCL	475	51	51
316	43	RCL	396	31	31	476	95	=
317	29	29	397	95	=	477	35	1/X
318	65	x	398	42	STD	478	91	R/S
319	43	RCL	399	37	37	479	00	0

Tape #6 Flexural Rigidity / Sample Problems

	0. 00	0. 00	0. 00	0. 00	00
	181.81114 09	181.81114 09	181.81114 09	181.81114 09	01
	10.346159 09	10.346159 09	10.346159 09	10.346159 09	02
	2.8969244 09	2.8969244 09	2.8969244 09	2.8969244 09	03
	0. 00	0. 00	0. 00	0. 00	04
	0. 00		0. 00		0. 00
	0. 00	0. 00	0. 00	0. 00	05
	0. 00	0. 00	0. 00	0. 00	06
	0. 00	0. 00	0. 00	0. 00	07
	0. 00	0. 00	0. 00	0. 00	08
	0. 00	0. 00	0. 00	0. 00	09
$[O_s]_s$	0. 00	$[O_4/90_4]_s$	0. 00	$[O_2/90_2/90_2]_s$	0. 00
	0. 00	0. 00	0. 00	0. 00	10
	0. 00	0. 00	0. 00	0. 00	11
	0. 00	0. 00	0. 00	0. 00	12
θ_1, β_1	0. 00	0. 00	90. 00	90. 00	13
	1. -03	1. -03	500. -06	750. -06	14
	40. 06	40. 06	0. 00	0. 00	15
	3.8447501 00	30.750001 03	θ_2, β_2	1. -03	16
	68. 06	68. 06	68. 06	68. 06	17
	2.8358135 03	22.65575 06	2.828126 03	22.625 06	18
	10.3 09	10.3 09	10.3 09	10.3 09	19
	5.6677823 03	22.65575 06	5.656251 03	22.625 06	20
z_c	0. 00	500. -06	0. 00	500. -06	21
	1. 00	875. -03	750. -03	281.25 -03	22
	1. 00	875. -03	1. 00	875. -03	23
	0. 00	0. 00	0. 00	0. 00	24
	0. 00	0. 00	0. 00	0. 00	25
	0. 00	0. 00	0. 00	0. 00	26
	181.81114 09	159.08475 09	160.37802 09	108.18108 09	27
	10.346159 09	9.0528889 09	31.779281 09	59.956555 09	28
	2.8969244 09	2.5348089 09	2.8969244 09	2.5348089 09	29
$\frac{12D_{ij}}{h^3}$	7.17 09	6.27375 09	7.17 09	6.27375 09	30
	0. 00	0. 00	0. 00	0. 00	31
	0. 00	0. 00	0. 00	0. 00	32
	8.2872928 -03	9.4711918 -03	9.3683286 -03	13.87939 -03	33
	145.63107 -03	166.43551 -03	47.278412 -03	25.042923 -03	34
	-2.320442 -03	-2.6519337 -03	-853.99478 -06	-586.78489 -06	35
d_{ij}	209.20502 -03	239.09145 -03	209.20502 -03	239.09145 -03	36
	0. 00	0. 00	0. 00	0. 00	37
	0. 00	0. 00	0. 00	0. 00	38
	13.426934 30	8.9949971 30	36.483153 30	40.652267 30	39
	0. 00	0. 00	0. 00	0. 00	40
	125. -06	125. -06	125. -06	125. -06	41
	49.487787 09	49.487787 09	49.487787 09	49.487787 09	42
	26.880431 09	26.880431 09	26.880431 09	26.880431 09	43
	85.73249 09	85.73249 09	85.73249 09	85.73249 09	44
$1 - (\frac{z}{h})^3$	19.710431 09	19.710431 09	19.710431 09	19.710431 09	45
	1. 00	875. -03	1. 00	875. -03	46
	0. 00	0. 00	0. 00	0. 00	47
	101.62602 -18	101.62602 -18	101.62602 -18	101.62602 -18	48
	0. 00	0. 00	0. 00	0. 00	49
$\frac{h^3}{12}$	1. -09	875. -12	875. -12	578.125 -12	50
	666.66667 -12	666.66667 -12	666.66667 -12	666.66667 -12	51
	0. 00	0. 00	0. 00	0. 00	52
	0. 00	0. 00	0. 00	0. 00	53
	12.004384 03	12.004384 03	12.004384 03	12.004384 03	54
	10.680652 03	10.680652 03	10.680652 03	10.680652 03	55
	-3.0691032 03	-3.0691032 03	-3.0691032 03	-3.0691032 03	56
	11.117842 03	11.117842 03	11.117842 03	11.117842 03	57
	60.646995 00	60.646995 00	60.646995 00	60.646995 00	58
	216.59641 00	216.59641 00	216.59641 00	216.59641 00	59

TAPE #7

FLEXURAL STRENGTH OF SYMMETRIC SANDWICH PLATES



USER INSTRUCTION

TAPE #7: FLEXURAL STRENGTH OF SYMMETRIC SANDWICH PLATES

STEP	PROCEDURE	ENTER	PRESS	DISPLAY
0	Results from Tape #6 must be in storage	--	--	--
1	Enter Moments M_k and calculate curvature k_j .	M_1	E	M_1
		M_2	R/S	M_2
		M_6	R/S	1.00
2	Calculate ply strains and the strength ratios at the outer face of each ply. These strength-strain ratios are based on mechanical strains, not the total strains.	--	A	S_1^M
		--	B	S_2^M
		--	C	S_3^M
		--	D	S_4^M

Tape* 7

Title FLEXURAL STRENGTH OF SYMMETRIC SANDWICH PLATES

KEYS	STORAGE MEMORIES		
A S_1^M	0	20 z_4	40 $z_i, b, b/2a, S_i$
	1 M_1	21 z_c	41 h_o
A'	2 M_2	22	42 S_1^M
	3 M_6	23	43 S_2^M
B S_2^M	4 k_1	24	44 S_3^M
	5 k_2	25	45 S_4^M
B'	6 k_6	26 M_6	46 $1 - \left(\frac{2z_c}{h}\right)^3$
	7 $\epsilon_1^M(z)$	27 $\epsilon_1^M(\theta_i)$	47 S_1^{-M}
C S_3^M	8 $\epsilon_2^M(z)$	28 $\epsilon_2^M(\theta_i)$	48 S_2^{-M}
	9 $\epsilon_6^M(z)$	29 $\epsilon_6^M(\theta_i)$	49 S_3^{-M}
C'	10 ϵ_1^N	30 $\epsilon_1^N(\theta_i) - e_L$	50 θ_i, S_4^{-M}
	11 ϵ_2^N	31 $\epsilon_2^N(\theta_i) - e_T$	51 $h/2, h^3/12$
D S_4^M	12 ϵ_6^N	32 $\epsilon_6^N(\theta_i)$	52 e_L
	13 θ_1	33 d_{11}	53 e_T
D'	14 z_1	34 d_{22}	54 G_{11}
	15 θ_2	35 d_{12}	55 G_{22}
E M_k	16 z_2	36 d_{66}	56 G_{12}
	17 θ_3	37 d_{16}	57 G_{66}
E'	18 z_3	38 d_{26}	58 G_1
	19 θ_4	39 $D, a, 1/a, \sqrt{S_i}$	59 G_2

Tape #7 Flexural Strength

M_k

000	76	LBL
001	15	E
002	42	STD
003	01	01
004	91	R/S
005	42	STD
006	02	02
007	91	R/S
008	42	STD
009	03	03

k_j

010	65	x
011	43	RCL
012	37	37
013	85	+
014	43	RCL
015	01	01
016	65	x
017	43	RCL
018	33	33
019	85	+
020	43	RCL
021	02	02
022	65	x
023	43	RCL
024	35	35
025	95	=
026	42	STD
027	04	04
028	43	RCL
029	01	01
030	65	x
031	43	RCL
032	35	35
033	85	+
034	43	RCL
035	02	02
036	65	x
037	43	RCL
038	34	34
039	85	+
040	43	RCL
041	03	03
042	65	x
043	43	RCL
044	38	38
045	95	=
046	42	STD
047	05	05
048	43	RCL
049	01	01
050	65	x
051	43	RCL
052	37	37
053	85	+
054	43	RCL
055	02	02
056	65	x
057	43	RCL
058	38	38
059	85	+
060	43	RCL
061	03	03
062	65	x
063	43	RCL
064	36	36
065	95	=
066	42	STD
067	06	06
068	01	1
069	95	=
070	91	R/S

S_1^M

071	76	LBL
072	11	A
073	43	RCL
074	13	13
075	42	STD
076	50	50
077	43	RCL
078	14	14
079	71	SBR

080	35	1/X
081	42	STD
082	47	47
083	43	RCL
084	40	40
085	42	STD
086	42	42
087	91	R/S

S_2^M

088	76	LBL
089	12	B
090	43	RCL
091	15	15
092	42	STD
093	50	50
094	43	RCL
095	16	16
096	71	SBR
097	35	1/X
098	42	STD
099	48	48
100	43	RCL
101	40	40
102	42	STD
103	43	43
104	91	R/S

S_3^M

105	76	LBL
106	13	C
107	43	RCL
108	17	17
109	42	STD
110	50	50
111	43	RCL
112	18	18
113	71	SBR
114	35	1/X
115	42	STD
116	49	49
117	43	RCL
118	40	40
119	42	STD
120	44	44
121	91	R/S

S_4^M

122	76	LBL
123	14	D
124	43	RCL
125	19	19
126	42	STD
127	50	50
128	43	RCL
129	20	20
130	71	SBR
131	35	1/X
132	42	STD
133	50	50
134	43	RCL
135	40	40
136	42	STD
137	45	45
138	91	R/S

$\epsilon_j^M(z_j)$

139	76	LBL
140	35	1/X
141	42	STD
142	40	40
143	65	x
144	43	RCL
145	04	04
146	95	=
147	42	STD
148	07	07
149	01	1
150	09	9
151	66	PAU
152	43	RCL
153	40	40
154	65	x
155	43	RCL
156	05	05
157	95	=
158	42	STD
159	08	08

160	43	RCL
161	40	40
162	65	x
163	43	RCL
164	06	06
165	95	=
166	42	STD
167	09	09

$\epsilon_j^M(\theta_j)$
 $-e_j$

168	02	2
169	49	PRD
170	50	50
171	43	RCL
172	10	10
173	85	+
174	43	RCL
175	11	11
176	95	=
177	55	-
178	02	2
179	95	=
180	42	STD
181	39	39
182	75	-
183	43	RCL
184	11	11
185	95	=
186	42	STD
187	40	40
188	65	x
189	43	RCL
190	50	50
191	39	CDS
192	85	+
193	43	RCL
194	39	39
195	85	+
196	43	RCL
197	12	12
198	65	x
199	43	RCL
200	50	50
201	38	SIN
202	55	+
203	02	2
204	75	-
205	43	RCL
206	52	52
207	95	=
208	42	STD
209	30	30
210	75	-
211	02	2
212	65	x
213	43	RCL
214	39	39
215	85	+
216	43	RCL
217	52	52
218	85	+
219	43	RCL
220	53	53
221	95	=
222	94	+/-
223	42	STD
224	31	31
225	43	RCL
226	12	12
227	65	x
228	43	RCL
229	50	50
230	39	CDS
231	75	-
232	43	RCL
233	40	40
234	65	x
235	02	2
236	65	x
237	43	RCL
238	50	50
239	38	SIN

Tape #7 Flexural Strength

240	95	=
241	42	STD
242	32	32
243	43	RCL
244	07	07
245	85	+
246	43	RCL
247	08	08
248	95	=
249	55	-
250	02	2
251	95	=
252	42	STD
253	39	39
254	75	-
255	43	RCL
256	08	08
257	95	=
258	42	STD
259	40	40
260	65	x
261	43	RCL
262	50	50
263	39	COS
264	85	+
265	43	RCL
266	39	39
267	85	+
268	43	RCL
269	09	09
270	65	x
271	43	RCL
272	50	50
273	38	SIN
274	55	-
275	02	2
276	95	=
277	42	STD
278	27	27
279	75	-
280	43	RCL
281	07	07
282	75	-
283	43	RCL
284	08	08
285	95	=
286	94	+/-
287	42	STD
288	28	28
289	43	RCL
290	09	09
291	65	x
292	43	RCL
293	50	50
294	39	COS
295	75	-
296	43	RCL
297	40	40
298	65	x
299	02	2
300	65	x
301	43	RCL
302	50	50
303	38	SIN
304	95	=
305	42	STD
306	29	29
307	33	X ²
308	65	x
309	43	RCL
310	57	57
311	85	+
312	43	RCL
313	54	54
314	65	x
315	43	RCL
316	27	27
317	33	X ²
318	85	+
319	02	2

320	65	x
321	43	RCL
322	56	56
323	65	x
324	43	RCL
325	27	27
326	65	x
327	43	RCL
328	28	28
329	85	+
330	43	RCL
331	55	55
332	65	x
333	43	RCL
334	28	28
335	33	X ²
336	95	=
337	42	STD
338	39	39
339	43	RCL
340	58	58
341	65	x
342	43	RCL
343	27	27
344	85	+
345	43	RCL
346	59	59
347	65	x
348	43	RCL
349	28	28
350	85	+
351	02	2
352	65	x
353	53	<
354	43	RCL
355	54	54
356	65	x
357	43	RCL
358	27	27
359	65	x
360	43	RCL
361	30	30
362	85	+
363	43	RCL
364	56	56
365	65	x
366	53	<
367	43	RCL
368	27	27
369	65	x
370	43	RCL
371	31	31
372	85	+
373	43	RCL
374	28	28
375	65	x
376	43	RCL
377	30	30
378	54	>
379	85	+
380	43	RCL
381	55	55
382	65	x
383	43	RCL
384	28	28
385	65	x
386	43	RCL
387	31	31
388	85	+
389	43	RCL
390	57	57
391	65	x
392	43	RCL
393	29	29
394	65	x
395	43	RCL
396	32	32
397	95	=
398	55	-
399	43	RCL

400	39	39
401	55	-
402	02	2
403	95	=
404	42	STD
405	40	40
406	01	1
407	75	-
408	43	RCL
409	54	54
410	65	x
411	43	RCL
412	30	30
413	33	X ²
414	75	-
415	02	2
416	65	x
417	43	RCL
418	56	56
419	65	x
420	43	RCL
421	30	30
422	65	x
423	43	RCL
424	31	31
425	75	-
426	43	RCL
427	55	55
428	65	x
429	43	RCL
430	31	31
431	33	X ²
432	75	-
433	43	RCL
434	57	57
435	65	x
436	43	RCL
437	32	32
438	33	X ²
439	75	-
440	43	RCL
441	58	58
442	65	x
443	43	RCL
444	30	30
445	75	-
446	43	RCL
447	59	59
448	65	x
449	43	RCL
450	31	31
451	95	=
452	55	-
453	43	RCL
454	39	39
455	85	+
456	43	RCL
457	40	40
458	33	X ²
459	95	=
460	34	FX
461	42	STD
462	39	39
463	75	-
464	43	RCL
465	40	40
466	95	=
467	42	STD
468	40	40
469	75	-
470	02	2
471	65	x
472	43	RCL
473	39	39
474	95	=
475	94	+/-
476	92	RTN
477	00	0
478	00	0
479	00	0

Tape #7 Flexural Strength / Sample Problems

	0. 00	0. 00	0. 00	0. 00	00
M_k	1. 00	1. 00	1. 00	1. 00	01
	0. 00	0. 00	0. 00	0. 00	02
	0. 00	0. 00	0. 00	0. 00	03
	8. 2872928-03	9. 4711918-03	9. 3683286-03	13. 87939-03	04
	-2. 320442-03	-2. 6519337-03	-853. 99478-06	-586. 78489-06	05
	0. 00	0. 00	0. 00	0. 00	06
	8. 2872928-06	9. 4711918-06	9. 3683286-06	13. 87939-06	07
	-2. 320442-06	-2. 6519337-06	-853. 99478-09	-586. 78489-09	08
	0. 00	0. 00	0. 00	0. 00	09
	0. 00	0. 00	0. 00	0. 00	10
	0. 00	0. 00	0. 00	0. 00	11
	0. 00	0. 00	0. 00	0. 00	12
	0. 00	0. 00	90. 00	90. 00	13
	1. -03	1. -03	500. -06	750. -06	14
	40. 06	40. 06	0. 00	0. 00	15
	3. 8447501 00	30. 750001 03	1. -03	1. -03	16
	68. 06	68. 06	68. 06	68. 06	17
	2. 8358135 03	22. 65575 06	22. 625 06	22. 625 06	18
	10. 3 09	10. 3 09	10. 3 09	10. 3 09	19
	5. 6677823 03	22. 65575 06	22. 625 06	22. 625 06	20
	0. 00	500. -06	0. 00	500. -06	21
	1. 00	875. -03	750. -03	281. 25-03	22
	1. 00	875. -03	1. 00	875. -03	23
	0. 00	0. 00	0. 00	0. 00	24
	0. 00	0. 00	0. 00	0. 00	25
	0. 00	0. 00	0. 00	0. 00	26
	8. 2872928-06	9. 4711918-06	9. 3683286-06	13. 87939-06	27
	-2. 320442-06	-2. 6519337-06	-853. 99478-09	-586. 78489-09	28
	0. 00	0. 00	0. 00	0. 00	29
	0. 00	0. 00	0. 00	0. 00	30
	0. 00	0. 00	0. 00	0. 00	31
	0. 00	0. 00	0. 00	0. 00	32
	8. 2872928-03	9. 4711918-03	9. 3683286-03	13. 87939-03	33
	145. 63107-03	166. 43551-03	47. 278412-03	25. 042923-03	34
	-2. 320442-03	-2. 6519337-03	-853. 99478-06	-586. 78489-06	35
	209. 20502-03	239. 09145-03	209. 20502-03	239. 09145-03	36
	0. 00	0. 00	0. 00	0. 00	37
	0. 00	0. 00	0. 00	0. 00	38
	1. 03	875. 00	964. 5143 00	667. 40582 00	39
	1. 03	875. 00	791. 97978 00	516. 39171 00	40
S^M	125. -06	125. -06	125. -06	125. -06	41
	1. 03	875. 00	835. 69432 00	374. 19028 00	42
	26. 880431 09	26. 880431 09	791. 97978 00	516. 39171 00	43
	85. 73249 09	85. 73249 09	85. 73249 09	85. 73249 09	44
	19. 710431 09	19. 710431 09	19. 710431 09	19. 710431 09	45
S^M	1. 00	875. -03	1. 00	875. -03	46
	1. 03	875. 00	4. 8092482 03	2. 2499333 03	47
	101. 62602-18	101. 62602-18	1. 1370488 03	818. 41992 00	48
	0. 00	0. 00	0. 00	0. 00	49
	0. 00	0. 00	0. 00	0. 00	50
	666. 66667-12	666. 66667-12	666. 66667-12	666. 66667-12	51
	0. 00	0. 00	0. 00	0. 00	52
	0. 00	0. 00	0. 00	0. 00	53
	12. 004384 03	12. 004384 03	12. 004384 03	12. 004384 03	54
	10. 680652 03	10. 680652 03	10. 680652 03	10. 680652 03	55
	-3. 0691032 03	-3. 0691032 03	-3. 0691032 03	-3. 0691032 03	56
	11. 117842 03	11. 117842 03	11. 117842 03	11. 117842 03	57
	60. 646995 00	60. 646995 00	60. 646995 00	60. 646995 00	58
	216. 59641 00	216. 59641 00	216. 59641 00	216. 59641 00	59

DATE
FILMED
-8